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7	Algorithm Theoretical Basis Document (ATBD
8	For
9	Land-Ice Along-Track Products Part 2:
10	Land-ice H(t)/ATL11
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26 Abstract

28	CM Foreword
29 30 31 32 33	This document is an Ice, Cloud, and Land Elevation Satellite-2 (ICESat-2) Project Science Office controlled document. Changes to this document require prior approval of the Science Development Team ATBD Lead or designee. Proposed changes shall be submitted in the ICESat-II Management Information System (MIS) via a Signature Controlled Request (SCoRe), along with supportive material justifying the proposed change.
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36	Questions or comments concerning this document should be addressed to:
37 38 39 40	ICESat-2 Project Science Office Mail Stop 615 Goddard Space Flight Center Greenbelt, Maryland 20771
41	

42	Preface
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44 45 46 47 48 49 50	This document is the Algorithm Theoretical Basis Document for the TBD processing to be implemented at the ICESat-2 Science Investigator-led Processing System (SIPS). The SIPS supports the ATLAS (Advance Topographic Laser Altimeter System) instrument on the ICESat-2 Spacecraft and encompasses the ATLAS Science Algorithm Software (ASAS) and the Scheduling and Data Management System (SDMS). The science algorithm software will produce Level 0 through Level 4 standard data products as well as the associated product quality assessments and metadata information.
51 52 53 54 55	The ICESat-2 Science Development Team, in support of the ICESat-2 Project Science Office (PSO), assumes responsibility for this document and updates it, as required, as algorithms are refined or to meet the needs of the ICESat-2 SIPS. Reviews of this document are performed when appropriate and as needed updates to this document are made. Changes to this document will be made by complete revision.
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# **Change History Log**

Revision Level	Description of Change	SCoRe No.	Date Approved
1.0	Initial Release		
1.0	Initial Release Changes for release 002. Calculate all crossovers (including near 88 S), determine the center of the y_atc search from the median of unique pair center locations.		

## List of TBDs/TBRs

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#### 1.0 INTRODUCTION

- 150 This document describes the theoretical basis and implementation of the level-3b land-ice
- processing algorithm for ATL11, which provides time series of surface heights. The higher-level
- products, providing gridded height, and gridded height change will be described in supplements
- to this document available in early 2020.
- 154 ATL11 is based on the ICESat-2 ATL06 Land-ice Height product, which is described
- elsewhere (Smith and others, 2019a, Smith and others, 2019b). ATL06 provides height estimates
- 156 for 40-meter overlapping surface segments, whose centers are spaced 20 meters along each of
- 157 ICESat-2's RPTs (reference pair tracks), but displaced horizontally both relative to the RPT and
- relative to one another because of small (a few tens of meters or less) imprecisions in the
- satellite's control of the measurement locations on the ground. ATL11 provides heights
- 160 corrected for these offsets between the reference tracks and the location of the ATLAS
- measurements. It is intended as an input for high-level products, ATL15 and ATL16, which
- will provide gridded estimates of ice-sheet height and height change, but also may be used alone,
- as a spatially-organized product that allows easy access to height-change information derived
- 164 from ICESat-2.
- 165 ATL11 employs a technique which builds upon those previously used to measured short-term
- elevation changes using ICESat repeat-track data. Where surface slopes are small and the
- geophysical signals are large compared to background processes (i.e., ice plains and ice shelves),
- some studies have subtracted the mean from a collection of height measurements from the same
- repeat track to leave the rapidly-changing components associated with subglacial water motion
- 170 (Fricker and others, 2007) or tidal flexure (Brunt and others, 2011). In regions where off-track
- surface slopes are not negligible, height changes can be recovered if the mean height and an
- estimate of the surface slope (Smith and others, 2009) are subtracted from the data, although in
- these regions the degree to which the surface slope estimate and the elevation-change pattern are
- independent is challenging to quantify.
- 175 ICESat-2's ATL06 product provides both surface height and surface-slope information each time
- it overflies its reference tracks. The resulting data are similar to that from the scanning laser
- altimeters that have been deployed on aircraft in Greenland and Antarctica for two decades
- 178 (cite), making algorithms originally developed for these instruments appropriate for use in
- interpreting ATLAS data. One example is the SERAC (Surface Elevation Reconstruction and
- 180 Change Detection) algorithm (Schenk & Csatho, 2012) provides an integrated framework for the
- derivation of elevation change from altimetry data. In SERAC, polynomial surfaces are fit to
- collections of altimetry data in small (< 1 km) patches, and these surfaces are used to correct the
- data for sub-kilometer surface topography. The residuals to the surface then give the pattern of
- elevation change, and polynomial fits to the residuals as a function of time give the long-term
- pattern of elevation change. The ATL11 algorithm is similar to SERAC, except that (1)
- polynomial fit correction is formulated somewhat differently, so that the ATL11 correction gives
- the surface height at the fit center, not the height residual, and (2) ATL11 does not include a
- polynomial fit with respect to time.

#### 2.0 BACKGROUND INFORMATION AND OVERVIEW

- 191 This section provides a conceptual description of ICESat-2's ice-sheet height measurements and
- 192 gives a brief description of the derived products.

#### 193 **2.1 Background**

- The primary goal of the ICESat-2 mission is to estimate mass-balance rates for the Earth's ice
- sheets. An important step in this process is the calculation of height change at specific locations
- on the ice sheets. In an ideal world, a satellite altimeter would exactly measure the same point
- on the earth on each cycle of its orbit. However, there are limitations in a spacecraft's ability to
- exactly repeat the same orbit and to point to the same location. These capabilities are greatly
- improving with technological advances but still have limits that need to be accounted for when
- 200 estimating precise elevation changes from satellite altimetry data. The first ICESat mission
- allowed estimates of longer-term elevation rates using along-track differencing, because
- 202 ICESat's relatively precise (50-150-m) pointing accuracy, precise (4-15 m) geolocation
- accuracy, and small (35-70-m) footprints allowed it to resolve small-scale ice-sheet topography.
- However, because ICESat had a single-beam instrument, its repeat-track measurements were
- reliable only for measuring the mean rate of elevation change, because shorter-term height
- 206 differences could be influenced by the horizontal dispersion of tracks on a sloping surface.
- 207 ICESat-2 makes repeat measurements over a set of 1387 reference ground tracks (RGTs),
- 208 completing a *cycle* over all of these tracks every 91 days. ICESat-2's ATLAS instrument
- 209 employs a split-beam design, where each laser pulse is divided six separate beams. The beams
- are organized into three *beam pairs*, with each separated from its neighbors by 3.3 km (**Figure**
- 211 2-1), each pair following a reference pair track (RPT) that is parallel to the RGT. The beams
- within each pair separated by 90 m, which means that each cycle's measurement over an RPT
- can determine the surface slope independently, and a height difference can be derived from
- any two measurements of an RPT. The 90-m spacing between the laser beams in each pair
- 215 is equal to twice the required RMS accuracy with which ICESat-2 can be pointed at its RPTs,
- 216 which means that for most, but not all, repeat measurements of a given RPT, the pairs of
- beams will overlap one another. To obtain a record of elevation change from the collection
- of paired measurements on each RPT, some correction is still necessary to account for the
- 219 effects of small-scale surface topography around the RPT in the ATL06 surface heights that
- appear as a result of this non-exact pointing. ATL11 uses a polynomial fit to the ATL06
- 221 measurements to correct for small-scale topography effects on surface heights that result
- from this non-exact pointing.
- 223 The accuracy of ICESat-2 measurements depends on the thickness of clouds between the
- satellite and the surface, on the reflectance, slope, and roughness of the surface, and on
- background noise rate which, in turn, depends on the intensity of solar illumination of the
- surface and the surface reflectance. It also varies from laser beam to beam, because in each
- of ICESat-2's beam pairs one beam (the "strong beam") has approximately four times the
- signal strength of the other (the "weak beam"). Parameters on the ATL06 product allow
- estimation of errors in each measurement, and allow filtering of most measurements with

large errors due to misidentification of clouds or noise as surface returns (blunders), but to enable higher precision surface change estimates, ATL11 implements further self-consistency checks that further reduce the effects of errors and blunders.

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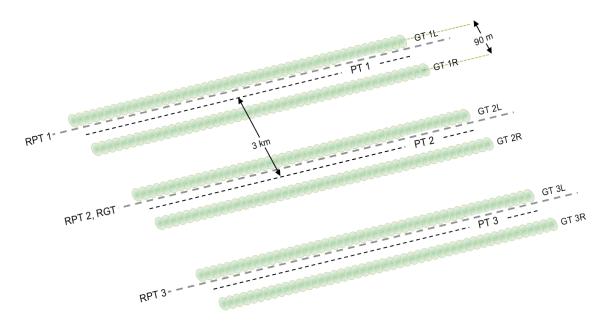
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Figure 2-1. ICESat-2 repeat-track schematic



Schematic drawing showing the pattern made by ATLAS's 6-beam configuration on the ground, for a track running from lower left to upper right. The 6 beams are grouped into 3 beam pairs with a separation between beams within a pair of 90m and a separation between beam pairs of 3.3 km. The RPTs (Reference Pair Tracks, heavily dashed lines in gray) are defined in advance of launch; the central RPT follows the RGT (Reference Ground Track, matching the nadir track of the predicted orbit). The Ground Tracks are the tracks actually measured by ATLAS (GT1L, GT1R, etc., shown by green footprints). Measured Pair Tracks (PTs, smaller dashed lines in black) are defined by the centers of the pairs of GTs, and deviate slightly from the RPTs because of inaccuracies in repeat-track pointing. The separation of GTs in each pair in this figure is greatly exaggerated relative to the separation of the PTs.

#### 2.2 Elevation-correction Coordinate Systems

We perform ATL11 calculations using the along-track coordinate system described in the ATL06 ATBD (Smith and others, 2019b, Smith and others, 2019a). The along-track coordinate is measured parallel to the RGT, starting at each RGT's origin at the equator. The across-track coordinate is measured to the left of the RGT, so that the two horizontal basis vectors and the local vertical vector form a right-handed coordinate system.

240 2.3 **Terminology:** 241 Some of the terms that we will use in describing the ATL11 fitting process and the data 242 contributing are: 243 *RPT*: Reference pair track 244 Cycle: ICESat-2 has 1387 distinct reference ground tracks, which its orbit covers every 91 days. One repeat measurement of these reference ground tracks constitutes a cycle. 245 246 ATL06 segment: A 40-meter segment fit to a collection of ATL03 photon-event data, as 247 described in the ATL06 ATBD 248 ATL06 pair: Two ATL06 segments from the same cycle with the same segment id. By 249 construction, both segments in the ATL06 pair have the same along-track coordinate, and are 250 separated by the beam-to-beam spacing (approximately 90 m) in the across-track direction 251 ATL11 RPT point: The expected location of each ATL11 point on the RPT, equivalent to the 252 beginning of every third geosegment on the RPT, or the center of every third ATL06 segment. 253 ATL11 reference point: an ATL11 RPT point shifted in the across-track direction to better match 254 the geometry of the available ATL06 data. 255 ATL11 fit: The data and parameters associated with a single ATL11 reference point. This 256 includes corrected heights from all available cycles 257 258 ATL11 calculates elevations and elevation differences based on collections of segments from the 259 same beam pair but from different cycles. ATL11 is posted every 60 m, which corresponds to 260 every third ATL06 segment id, and includes ATL06 segments spanning three segments before 261 and after the central segment, so that the ATL11 uses data that span 120 m in the along-track 262 direction. ATL11 data are centered on reference points, which has the same along-track coordinate as its central ATL06 segment, but is displaced in the across-track direction to better 263

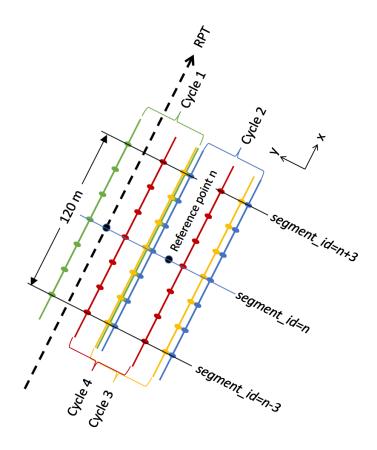
Figure 2-2. ATL06 data for an ATL11 reference point

match the locations of the ATL06 measurements from all of the cycles present (see section

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3.1.3).



Schematic of ATL06 data for an ATL11 reference point centered on segment n, based on data from four cycles. The segment centers span 120 m in the along-track data, and the cycles are randomly displaced from the RPT in the across-track direction. The reference point has an along-track location that matches that of segment n, and an across-track position chosen to match the displacements of the cycles.

## 2.4 Repeat and non-repeat cycles in the ICESat-2 mission

In the early part of the ICESat-2 mission, an error in the configuration of the start trackers prevented the instrument from pointing precisely at the RGTs. As a result, all data from cycles 1 and 2 were measured between one and two kilometers away from the RGTs, with offsets that varied in time and as a function of latitude. The measurements from cycles 1 and 2 still give high-precision measurements of surface height, but repeat-track measurements from ICESat-2 begin during cycle 3, in April of 2019. ATL11 files will be generated for ATL06 granules from cycles 1 and 2, but these will contain only one cycle of data, plus crossovers, because the measurements from these cycles (which are displaced from the RPTs by several kilometers) will not be repeated. We expect the measurements from cycles 1 and 2 to be useful as a reduced-resolution (compared to ATL06) mapping of the ice sheet, which may prove useful in DEM generation and in comparisons with other altimetry missions. For cycles 3 and after, each

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- 279 ATL11 granule will contain all available cycles for each RGT (i.e. from cycle 3 onwards), and
- will contain crossovers between the repeat cycles and cycles 1 and 2.
- Outside the polar regions, ICESat-2 is pointed to minimize gaps between repeat measurements,
- and so does not make repeat measurements over its ground tracks. ATL11 is only calculated
- 283 within the repeat-pointing mask (see Figure ???), which covers areas poleward of 60°N and
- 284 60°S.

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## 2.5 Physical Basis of Measurements / Summary of Processing

- Surface slopes on the Antarctic and Greenland ice sheets are generally small, with magnitudes
- less than two degrees over 99% of Antarctica's area. Smaller-scale (0.5-3 km) undulations,
- generated by ice flow over hilly or mountainous terrain may have amplitudes of up to a few
- degrees. Although we expect that the surface height will change over time, slopes and locations
- of these smaller-scale undulation are likely controlled by underlying topography and should
- remain essentially constant over periods of time comparable with the expected 3-7 duration of
- the ICESat-2 mission. This allows us to use estimates of ice-sheet surface shape derived from
- data spanning the full mission to correct for small (<130-m) differences in measurement
- locations between repeat measurements of the same RPT, to produce records of height change
- 296 for specific locations. To account for changes in the ice-sheet surface slope associated with
- 297 gradients in thinning, we also solve for the rate of surface-slope change, when sufficient data are
- available. Further, we can use the surface slope estimates in ATL06 to determine whether
- 299 different sets of measurements for the same fit center are self-consistent: We can assume that if
- an ATL06 segment shows a slope significantly different from others measured near the same
- reference point it likely is in error. The combination of parameters from ATL06 and these self-
- 302 consistency checks allows us to generate time series based on the highest-quality measurements
- for each reference point, and our reference surface calculation lets us correct for small-scale
- 304 topography and to estimate error magnitudes in the corrected data.

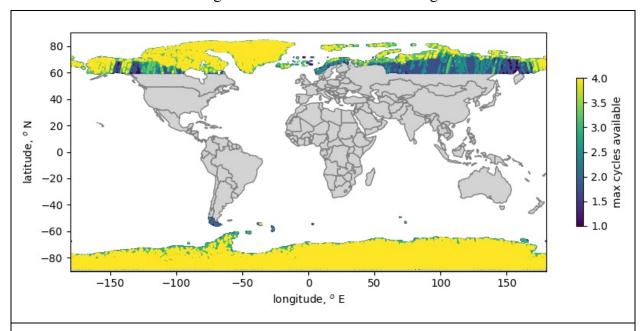
#### 2.5.1 Choices of product dimensions

- We have chosen a set of dimensions for the ATL11 fitting process with the goal of creating a
- product that is conveniently sized for analysis of elevation changes, while still capturing the
- details of elevation change in outlet glaciers. The assumption that ice-sheet surface can be
- approximated by a low-degree polynomial becomes untenable as data from larger and larger
- areas are included in the calculation; therefore we use data from the smallest feasible area to
- define our reference surface, while still including enough data to reduce the sampling error in the
- data and to allow for the possibility that at least one or two will encounter a flat surface, which
- 313 greatly improves the chances that each cycle will be able to measure surface comparable to one
- another. Each ATL11 point uses data from an area up to 120 m in the along-track direction by
- 315 up to 130 m in the across-track direction. We have chosen the cross-track search distance
- 316 (L<sub>search XT</sub>) to be 65 m, approximately equal to half the beam spacing, plus three times the
- observed 6.5 m standard deviation of the across-track pointing accuracy for cycles 3 and 4 in
- Antarctica. We chose the across-track search distance (L<sub>search AT</sub>) to be 60 m, approximately

equal to L<sub>search\_XT</sub>, so that the full L<sub>search\_AT</sub> search window spans three ATL06 segments before and after the central segment for each reference point. The resulting along-track resolution is around one third that of ATL06, but still allows 6-7 distinct elevation-change samples across a small (1-km) outlet glacier.

#### 2.6 Product coverage

Figure 2-3. Potential ATL11 coverage

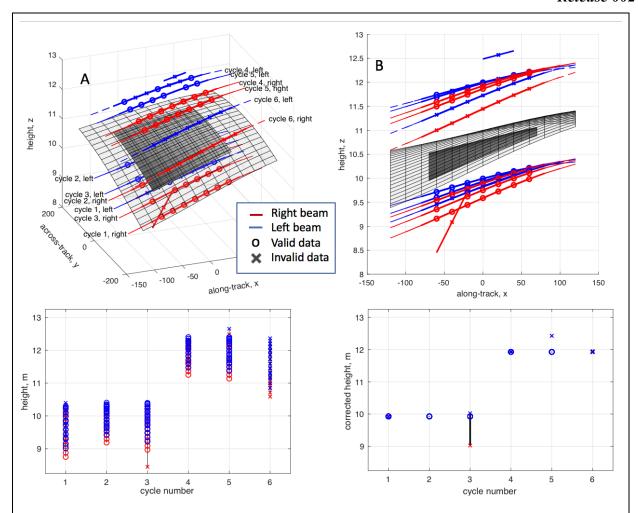


Maximum number of valid repeat measurements from an ATL11 file for each 10-km segment of pair track 2. Yellower colors indicate areas where ICESat-2 has systematically pointed at the RGTs.

Over the vegetated parts of the Earth, ICESat-2 makes spatially dense measurements, measuring tracks parallel to the reference tracks in a strategy that will eventually measure global vegetation with a track-to-track spacing better than 1 km. Because ATL11 relies upon repeat measurements over reference tracks to allow the calculation of its reference surfaces, ATL11 is generated for ICESat-2 subregions 3-5 and 10-12 (global coverage, north and south of 60 degrees). Repeat measurements are limited to Antarctica, Greenland, and the High Arctic islands (Figure 2-3), although in other areas the fill-in strategy developed for vegetation measurements allows some repeat measurements. In regions where ICESat-2 was not pointed to the repeat track, most ATL11 reference points will provide one measurement close to the RPT. Crossover data are available for many of these points, though their distribution in time is not regular. A future update to the product may provide crossover measurements for lower-latitude areas, but the current product format is not designed to allow this.

336	3.0 ALGORITHM THEORY: DERIVATION OF LAND ICE H (1)/ATLIT (L3B)
337 338 339 340 341	In this section, we describe in detail the algorithms used in calculating the ATL11 land-ice parameters. This product is intended to provide time series of surface heights for land-ice and ice-shelf locations where ICESat-2 operates in repeat-track mode ( <i>i.e.</i> for polar ice), along with parameters useful in determining whether each height estimate is valid or a result of a variety of potential errors (see ATL06 ATBD, section 1).
342 343 344 345 346 347 348	ATL11 height estimates are generated by correcting ATL06 height measurements for the combined effects of short-scale (40-120-m) surface topography around the fit centers and small (up to 130-m) horizontal offsets between repeat measurements. We fit a polynomial reference surface to height measurements from different cycles as a function of horizontal coordinates around the fit centers, and use this polynomial surface to correct the height measurements to the fit center. The resulting values reflect the time history of surface heights at the reference points, with minimal contributions from small-scale local topography.
349 350 351 352 353 354 355 356 357 358 359	In this algorithm, for a set of reference points spaced every 60 meters along each RPT (centered on every third segment center), we consider all ATL06 segments with centers within 60 m along track and 65 m across-track of the reference point, so that each ATL11 fit contains as many as seven distinct along-track segments from each laser beam and cycle. We select a subset of these segments with consistent ATL06 slope estimates and small error estimates, and use these segments to define a time-variable surface height and a polynomial surface-shape model. We then use the surface-shape model to calculate corrected heights for the segments from cycles not included in the initial subset. We propagate errors for each of these steps to give formal errors estimates that take into account the sampling error from ATL06, and propagate the geolocation errors with the slope of the surface-shape model to give an estimate of systematic errors in the height estimates.

Figure 3-1. ATL11 fitting schematic



Schematic of the ATL11 fitting strategy. A and B show different renderings of the same set of data, A in perspective view and B from along the y (along-track axis). Lines show simulated ATL11 profiles; symbols show segment centers for segments within 60 m of the fit center (at x=y=0). Red lines and symbols indicate left beams, blue indicate right beams. 'o' markers indicate valid data segments, 'x' markers indicate invalid data segments. We plot the unperturbed, true surface height as a light-colored semi-transparent mesh, and the recovered surface height as a gray-shaded, opaque surface, shifted vertically to match the true surface. The gray surface shows the fit correction surface, offset vertically to match the true surface. C shows the uncorrected heights as a function of cycle number, and D shows the corrected heights (bottom), plotted for each repeat.

Figure 3-1 shows a schematic diagram of the fitting process. In this example, we show simulated ATL06 height measurements for six 91-day orbital cycles over a smooth ice-sheet surface (transparent grid). Between cycles 3 and 4, the surface height has risen by 2 m. Two of the segments contain errors: The weak beam for one segment from repeat 3 is displaced downward and has an abnormal apparent slope in the x direction, and one segment from repeat 5 is displaced upwards, so that its pair has an abnormal apparent slope in the y direction. Segments falling within the across and along-track windows of the reference point (at x=y=0 in this plot) are selected, and fit with a polynomial reference surface (shown in gray). When plotted as a

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function of cycle number (panel C), the measured heights show considerable scatter but when corrected to the reference surface (panel D), each cycle shows a consistent height, and the segments with errors are clearly distinct from the accurate measurements.

#### 3.1 Input data editing

Each ATL06 measurement includes location estimates, along- and across-track slope estimates, and PE (Photon-Event)-height misfit estimates. To calculate the reference surface using the most reliable subset of available data, we perform tests on the surface-slope estimates and error statistics from each ATL06-pair to select a self-consistent set of data. These tests determine whether each pair of measurements is *valid* and can be used in the reference-shape calculation or is *invalid*. Segments from invalid pairs may be used in elevation-change calculations, but not in the reference-shape calculation.

A complete flow chart of the data-selection process is shown in Figure 3-2, and the parameters used to make these selections and their values are listed in Table 3-1.

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Table 3-1 Parameter Filters to determine the validity of segments for ATL11 estimates

complex_surface _flag	Segment parameter	Filter strategy	Section
0	ATL06_quality_summary	ATL06_quality_summary =0 (indicates high-quality segments)	3.1.1
1	SNR_significance	SNR_significance < 0.02 (indicates low probability of surface-detection blunders)	3.1.1
0 or 1	Along-track differences	Minimum height difference between the endpoints of a segment and the middles of its neighbors must be < 2 m (for smooth surfaces) or < 10 m (for complex surfaces)	3.1.1
0 or 1	h_li_sigma	$h_li_sigma < max(0.05, 3*median(h_li_sigma))$	3.1.1
0 or 1	Along-track slope	r_slope_x <3 slope_tolerance_x	3.1.2
0 or 1	Across-track slope	$ r\_slope\_y  < 3$ $slope\_tolerance\_y$	3.1.2

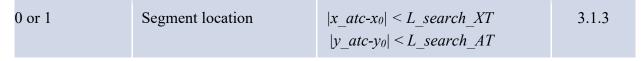
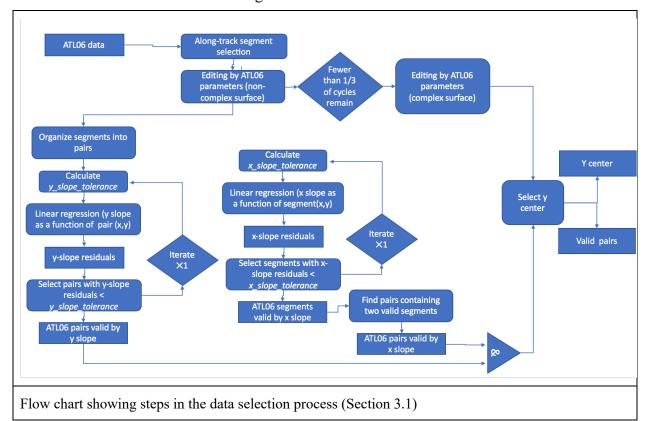


Figure 3-2. Data selection



385 3.1.1 Input data editing using ATL06 parameters

For each reference point, we collect all ATL06 data from all available repeat cycles that have  $segment\_id$  values within  $\pm 3$  of the reference point (inclusive) and that are on the same rgt and pair track as the reference point. The  $segment\_id$  criterion ensures that the segment centers are within  $\pm 60$  m of the reference point in the along-track direction. We next check that the ATL06 data are close to the pre-defined reference track, by rejecting all ATL06 segments that are more than 500 m away from the nominal pair across-track coordinates (-3200, 0, and 3200 meters for right, center, and left pairs, respectively). This removes data that were intentionally or accidentally collected with ATLAS pointed off nadir (i.e. for calibration scan maneuvers).

ATL06 contains some segments with signal-finding blunders (Smith et al., 2019). To avoid having these erroneous segments contaminate ATL11, we filter using one of two sets of tests, depending on surface roughness. We identify high-quality ATL06 segments, using parameters that depend on whether the surface is identified as smooth or rough, as follows:

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- 398 1) For smooth ice-sheet surfaces, we use the ATL06 *ATL06 quality summary* parameter,
- 399 combined with a measure of along-track elevation consistency, at min dh, that is calculated as
- 400 part of ATL11. ATL06 quality summary is based on the spread of the residuals for each
- segment, the along-track surface slope, the estimated error, and the signal strength. Zero values
- indicate that no error has been found. We define the along-track consistency parameter
- 403 at min dh as the minimum absolute difference between the heights of the endpoints of each
- segment and the center heights of the previous and subsequent segments. Its value will be small
- if a segment's height and slope are consistent with at least one of its neighbors. For smooth
- surfaces, we require that the at min dh values be less than 2 m. Over smooth ice-sheet surfaces,
- 407 the 2-m threshold eliminates most blunders without eliminating a substantial number of high-
- 408 quality data points.
- 2) For rough, crevassed surfaces, the smooth-ice strategy may not identify a sufficient number of
- 410 pairs for ATL11 processing to continue. If fewer than one third of the original cycles remain
- after the smooth-surface criteria are applied, we relax our criteria, using the signal-to-noise ratio
- 412 (based on the ATL06 segment stats/snr significance parameter) to select the pairs to include in
- 413 the fit, and require that the at min dh values be less than 10 m. If we relax the criteria in this
- 414 way, we mark the reference point as having a complex surface using the
- 415 ref surf/complex surface flag, which limits the degree of the polynomial used in the reference
- 416 surface fitting to 0 or 1 in each direction.
- For either smooth or rough surfaces, we perform an additional check using the magnitude of
- 418 h li sigma for each segment. If any segment's value is larger than three times the maximum of
- 419 0.05 m and the median h li sigma for the valid segments for the current reference point, it is
- marked as invalid. The limiting 0.05 m value prevents this test from removing high-quality data
- over smooth ice-sheet surfaces, where errors are usually small.
- Each of these tests applies to values associated with ATL06 segments. When the tests are
- complete, we check each ATL06 pair (i.e. two segments for the same along-track location from
- 424 the same cycle) and if either of its two segments has been marked as invalid, the entire pair is
- 425 marked as invalid.

#### 3.1.2 Input data editing by slope

- The segments selected in 3.1.1 may include some high-quality segments and some lower-quality
- segments that were not successfully eliminated by the data-editing criteria. We expect that the
- 429 ATL06 slope fields (dh fit dx, and dh fit dy) for the higher-quality data should reflect the
- shape of an ice-sheet surface with a spatially consistent surface slope around each reference
- point, but that at least some of lower-quality data should have slope fields that outliers relative to
- 432 this consistent surface slope. In this step, we assume that the slope may vary linearly in x and y,
- and so use residuals between the slope values and a regression of the slope values against x and y
- 434 to identify the data with inconsistent slope values. The data with large residuals are marked as
- 435 invalid.

- 436 Starting with valid pairs from 3.2.1, we first perform a linear regression between the y slopes of
- 437 the pairs and the pair-center x and y positions. The residuals to this regression define one
- 438 *y slope residual* for each pair. We compare these residuals against a *y slope tolerance*:

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 $y\_slope\_tolerance = max(0.01, 3 median (dh\_fit\_dy\_sigma), 3 RDE$  1  $(y\_slope\_residuals))$ 

- Here RDE is the Robust Difference Estimator, equal to half the difference between the 16th and
- 84<sup>th</sup> percentiles of a distribution, and the minimum value of 0.01 ensures that this test does not
- remove high-quality segments in regions where the residuals are very consistent. If any pairs
- have a y slope residual greater than y slope tolerance, we remove them from the group of valid
- pairs, then repeat the regression, recalculate y slope tolerance, and retest the remaining pairs.
- We then return to the pairs marked as *valid* from 3.1.1, and perform a linear regression between
- the x slopes of the segments within the pairs and the segment-center x and y positions. The
- residuals to this regression define one x slope residual for each segment. We compare these
- residuals against an x slope tolerance, calculated in the same way as (1), except using segment x
- slopes and residuals instead of pair y slopes. As with the y regression, we repeat this procedure
- once if any segments are eliminated in the first round.
- 450 After both the x and y regression procedures are complete, each pair of segments is marked as
- 451 *valid* if both of its x residuals are smaller than *slope tolerance* x and its y residual is smaller than
- 452 slope tolerance y.

453

#### 3.1.3 Spatial data editing

- The data included in the reference-surface fit fall in a "window" defined by a  $2L_{search\ XT}$  by
- 455  $2L_{search\ AT}$  rectangle, centered on each reference point. Because the across-track location of the
- 456 repeat measurements for each reference point are determined by the errors in the repeat track
- pointing of ATLAS, a data selection window centered on the RPT in the y direction will not
- 458 necessarily capture all of the available cycles of data. To improve the overlap between the
- window and the data, we shift the reference point in the y direction so that the window includes
- as many valid beam pairs as possible. We make this selection after the parameter-based (3.1.1)
- and slope-based (3.1.2) editing steps because we want to maximize the number high-quality pairs
- to the state of th
- included, without letting the locations of low-quality segments influence our choice of the
- 463 reference-point shift.
- We select the across-track offset for each reference point by searching a range of offset values, δ,
- around the RPT to maximize the following metric:

 $M(\delta)$  = [number of unique valid pairs entirely contained in  $\delta \pm L_{search\ XT}$ ]

- + [number of unpaired segments contained in  $\delta \pm L_{search XT}$ ]/100
- 466 Maximizing this metric allows the maximum number of pairs with two valid segments to be
- included in the fit, while also maximizing the number of segments included close to the center of
- 468 the fit. If multiple values of  $\delta$  have the same M value we choose the median of those  $\delta$  values.
- The across-track coordinate of the adjusted reference point is then  $y_0 + \delta_{max}$ , where  $y_0$  is the
- across-track coordinate of the unperturbed reference point. After this adjustment, the segments

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- 471 in pairs that are contained entirely in the across-track interval  $\delta \pm L_{search\ XT}$  are identified as
- 472 *valid* based on the spatial search.
- The location of the adjusted reference point is reported in the data group for each pair track, with
- 474 corresponding local coordinates in the ref surf subgroup: /ptx/ref surf/x atc, /ptx/ref surf/y atc.

#### 475

476

#### 3.2 Reference-Surface Shape Correction

- To calculate the reference-surface shape correction, we construct the background surface shape
- 478 from valid segments selected during 3.1 and 3.2, using a least-squares inversion that separates
- 479 surface-shape information from elevation-change information. This produces surface shape-
- 480 corrected height estimates for cycles containing at least one valid pair, and a surface-shape
- 481 model that we use in later steps (3.4, 3.6) to calculate corrected heights for cycles that contain no
- valid pairs and to calculate corrected heights for crossing tracks.

## 483 **3.2.1** Reference-surface shape inversion

- 484 The reference-shape inversion solves for a reference surface and a set of corrected-height values
- 485 that represent the time-varying surface height at the reference point. The inversion involves
- 486 three matrices:
- 487 (i): a polynomial surface shape matrix, S, that describes the functional basis for the spatial part of
- 488 the inversion:

$$\mathbf{S} = \left[ \left( \frac{x - x_0}{l_0} \right)^p \left( \frac{y - y_0}{l_0} \right)^q \right]$$

- Here  $x_0$  and  $y_0$  are equal to the along-track coordinates of the adjusted reference point,
- 490 /ptx/ref surf/x atc and /ptx/ref surf/y atc, respectively. S has one column for each permutation
- of p and q between zero and the degree of the surface polynomial in each dimension, but does
- not include a p=q=0 term. The degree is chosen to be no more than 3 (in the along-track
- direction) or 2 (in the across-track direction), and to be no more than the number of distinct pair-
- center y values (in the across-track direction) or more than 1 less than the number of distinct x
- values (in the along-track direction) in any cycle, with distinct values defined at a resolution of
- 496 20 m in each direction. The scaling factor,  $l_0$ , ensures that the components of S are on the order
- 497 of 1, which improves the numerical accuracy of the computation. We set  $l_0=100$  m, to
- 498 approximately match the intra-pair beam spacing.
- 499 (ii): a matrix that encodes the repeat structure of the data, that accounts for the height-change
- 500 component of the inversion:

$$\mathbf{D} = [\delta(i,1), \delta(i,2), \dots, \delta(i,N)]$$

- Here  $\delta$  is the delta function, equal to 1 when its arguments are equal, zero otherwise, and i is an
- index that increments by one for each distinct cycle in the selected data.

503 (iii): a matrix that describes the linear rate of change in the surface slope over the course of the 504 mission:

$$\mathbf{S}_{t} = \left[ \left( \frac{x - x_0}{l_0} \right) \left( \frac{t - t_0}{\tau} \right), \left( \frac{y - y_0}{l_0} \right) \left( \frac{t - t_0}{\tau} \right) \right]$$
 5

- Here  $t_0$  is equal to slope change t0, the mid-point of the mission at the time that ATL11 is
- generated, halfway between start repeat track pointing (the beginning of cycle 3) and either the
- end of the mission or the processing time (slope change t0 is an attribute of each ATL11
- 508 *file*). This implies that on average,  $(t t_0)$  will have a zero mean. The time-scaling factor,  $\tau$ , is
- equal to one year (86400\*365.25 seconds). This component will only be included in ATL11
- once eight complete cycles of data are available on the RGTs (after cycle 10 of the mission).
- The surface shape, slope change, and height time series are estimated by forming a composite
- design matrix, **G**, where

$$\mathbf{G}=[\mathbf{S}\ \mathbf{S}_{\mathsf{t}}\ \mathbf{D}],$$

- and a covariance matrix, C, containing the squares of the segment-height error estimates on its
- diagonal. The surface-shape polynomial and the height changes are found:

$$[s, s_t, z_c] = G^{-g}z$$
  
where 
$$7$$
$$G^{-g} = [G^TC^{-1}G]^{-1}G^TC^{-1}$$

- The notation []<sup>-1</sup> designates the inverse of the quantity in brackets, and z is the vector of segment
- 516 heights. The parameters derived in this fit are s, a vector of surface-shape polynomial
- coefficients,  $\mathbf{s}_t$ , the mean rate of surface-slope change, and  $\mathbf{z}_c$ , a vector of corrected height values,
- giving the height at  $(lat_0, lon_0)$  as inferred from the height measurements and the surface
- polynomial. The matrix  $G^{-g}$  is the generalized inverse of G. The values of S are reported in the
- 520 ref surf/poly ref surf parameter, as they are calculated from (6), with no correction made for the
- scaling in (3). The values for the slope-change rates are reported in ref surf/slope change rate,
- after rescaling to units of *years*<sup>-1</sup>.

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## 3.2.2 Misfit analysis and iterative editing

- If blunders remain in the data input to the reference-surface calculation, they can lead to
- 525 inaccurate reference surfaces. To help remove these blunders, we iterate the inversion procedure
- 526 in 3.2.1, eliminating outlying data points based on their residuals to the reference surface.
- To determine whether outliers may be present, we calculate the chi-squared misfit between the
- data and the fit surface based on the data covariance matrix and the residual vector, r:

$$\chi^2 = r^T \mathbf{C}^{-1} r \tag{8}$$

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- To determine whether this misfit statistic indicates consistency between the polynomial surface
- and the data we use a P statistic, which gives the probability that the given  $\chi^2$  value would be
- obtained from a random Gaussian distribution of data points with a covariance matrix C. If the
- probability is less than 0.025, we perform some further filtering/editing: we calculate the RDE of
- 533 the scaled residuals, eliminate any pairs containing a segment whose scaled residual magnitude is
- larger than three times that value, and repeat the remaining segments.
- After each iteration, any column of G that has a uniform value (i.e. all the values are the same) is
- eliminated from the calculation, and the corresponding value of the left-hand side of equation 7
- is set to zero. Likewise, if the inverse problem has become less than overdetermined (i.e., the
- number of data is smaller than the number of unknown values they are constraining), the
- polynomial columns of G are eliminated one by one until the number of data is greater than the
- number of unknowns. Columns are eliminated in descending order of the sum of x and y
- degrees, and when there is a tie between columns based on this criterion, the column with the
- 542 larger y degree is eliminated first.
- 543 This fitting procedure is continued until no further segments are eliminated. If more than three
- complete cycles that passed the initial editing steps are eliminated in this way, the surface is
- assumed to be too complex for a simple polynomial approximation, and we proceed as follows:
- 546 (i) the fit and its statistics are reported based on the complete set of pairs that passed 547 the initial editing steps (valid pairs), using a planar (x degree = y degree = 1) fit in x and y.
- 548 (ii) the ref surf/complex surface flag is set to 1.
- The misfit parameters are reported in the *ref surf* group: The final chi-squared statistic is
- reported as ref surf/misfit chi2r, equal to the chi-squared statistic divided by the number of
- degrees of freedom in the solution; the final RMS of the scaled residuals is reported as
- 552 ref surf/misfit rms.

553

#### 3.3 Reference-shape Correction Error Estimates

- We first calculate the errors in the corrected surface heights for segments included in the
- reference-surface fit. We form a second covariance matrix, C<sub>1</sub>, whose diagonal elements are the
- maximum of the squares of the segment errors and  $\langle r^2 \rangle$ . We estimate the covariance matrix for
- the height estimates:

$$\mathbf{C}_m = \mathbf{G}^{-g} \mathbf{C}_1 \mathbf{G}^{-gT}$$

- The square roots of the diagonal values of  $C_{\rm m}$  give the estimated errors in the surface-polynomial
- and height estimates due to short-spatial-scale errors in the segment heights. If there are  $N_{coeff}$
- coefficients in the surface-shape polynomial, and  $N_{shape-cycles}$  cycles included in the surface-shape
- 561 fit, then the first  $N_{coeff}$  diagonal elements of  $C_{m}$  give the square of the errors in the surface-shape
- polynomial and the last  $N_{shape-cycles}$  give the errors in the surface heights for the cycles included in
- 563 the fit. The portion of C<sub>m</sub> that refers only to the surface shape and surface-shape change
- 564 components is  $C_{m,s}$ .

#### 3.4 Calculating corrected height values for repeats with no selected pairs

- Once the surface polynomial has been established from the edited data set, corrected heights are
- calculated for the unselected cycles (i.e. those from which all pairs were removed in the editing
- steps): For the segments among these cycles, we form a new surface and slope-change design
- matrix,  $[S, S_t]$  and multiply it by  $[s, s_t]$  to give the surface-shape correction:

$$\mathbf{z}_c = \mathbf{z} - [\mathbf{S}, \mathbf{S}_t][\mathbf{s}, \mathbf{s}_t]$$

- Here s is the surface-shape polynomial, and  $s_t$  is the slope-change-rate estimate. This gives up to
- 571 fourteen corrected-height values per unselected cycle. From among these, we select the segment
- with the minimum error, as calculated in the next step.

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573 The height errors for segments from cycles not included in the surface-shape fit are calculated:

$$\sigma_{z,c}^2 = diag([\mathbf{S}, \mathbf{S}_t]\mathbf{C}_{m,s}[\mathbf{S}, \mathbf{S}_t]^T) + \sigma_z^2$$

- Here  $\sigma_z$  is the error in the segment height, and  $\sigma_{z,c}$  is the error in the corrected height. The
- results of these calculations give a height and a height error for each unselected segment. To
- obtain a corrected elevation for each repeat that contains no selected pairs, we identify the
- segment from that repeat that has the smallest error estimate, and report the value  $z_c$  as that
- repeat's ptx/h corr, and use  $\sigma_{z,c}$  as its error (/ptx/h corr sigma).

## 579 3.5 Calculating systematic error estimates

- The errors that have been calculated up to this point are due to errors in fitting segments to
- 581 photon-counting data and due to inaccuracies in the polynomial fitting model. Additional error
- components can result from more systematic errors, such as errors in the position of ICESat-2 as
- derived from POD, and pointing errors from PPD. These are estimated in the ATL06
- 584 sigma geo xt, sigma geo at, and sigma geo r parameters, and their average for each repeat is
- reported in the *cycle stats* group under the same parameter names. The geolocation component
- of the total height is the product of the geolocation error and the surface slope, added in
- 587 quadrature with the vertical height error:

$$\sigma_{h,systematic} = \left[ \left( \frac{dh}{dx} \sigma_{geo,AT} \right)^2 + \left( \frac{dh}{dy} \sigma_{geo,XT} \right)^2 + \sigma_{geo,T}^2 \right]^{1/2}$$
 12

- 588 For selected segments, which generally come from pairs containing two high-quality height
- estimates, dh/dy is estimated from the ATL06 dh fit dy parameter. For unselected segments, it is
- based on the y component of the reference-surface slope, as calculated in section 4.2.
- The error for a single segment's corrected height is:

$$\sigma_{h,total} = \left[\sigma_{h,systematic}^2 + \sigma_{h,c}^2\right]^{1/2}$$

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- This represents the total error in the surface height for a single corrected height. In most cases,
- error estimates for averages of ice-sheet quantities will depend on errors from many segments
- from different reference points, and the spatial scale of the different error components will need
- 595 to be taken into account in error propagation models. To allow users to separate these effects,
- we report both the uncorrelated error, /ptx/h corr sigma, and the component due only to
- 597 systematic errors, /ptx/h corr sigma systematic. The total error is the quadratic sum of the two,
- as described in equation 13.

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#### 3.6 Calculating shape-corrected heights for crossing-track data

- 600 Locations where groundtracks cross provide opportunities to check the accuracy of
- measurements by comparing surface-height estimates between the groundtracks, and also offers
- the opportunity to generate elevation-change time series that have more temporal detail than the
- 603 91-day repeat cycle can offer for repeat-track measurements.
- At these crossover points, we use the reference surface calculated in 3.5 to calculate corrected
- elevations for the crossing tracks. We refer to the track for which we have calculated the
- reference surface as the *datum* track, and the other track as the *crossing* track. To calculate
- 607 corrected surface heights for the crossing ICESat-2 orbits, we first select all data from the
- 608 crossing orbit within a distance L search XT of the updated reference point on the datum track.
- For most datum reference points, this will yield no crossing data, in which case the calculation
- for that datum point terminates. If crossing data are found, we then calculate the coordinates of
- these points in the reference point's along-track and across-track coordinates. This calculation
- begins by transforming the crossing-track data into local northing and easting coordinates
- relative to the datum reference-point location:

$$\delta N_c = \frac{\pi R_e}{180} (lat_c - lat_d)$$

$$\delta E_c = \frac{\pi R_e}{180} (lon_c - lon_d) \cos(lat_c)$$
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- Here  $(lat_d, lon_d)$  are the coordinates of the adjusted datum reference point,  $(lat_c, lon_c)$  are the
- coordinates of the points on the crossing track, and  $R_e$  is the local radius of the WGS84 ellipsoid.
- We then convert the northing and easting coordinates into along-track and across-track
- 617 coordinates based on the azimuth  $\phi$  of the datum track:

$$x_c = \delta N_c \cos(\phi) + \delta E_c \sin(\phi)$$

$$y_c = \delta N_c \sin(\phi) - \delta E_c \cos(\phi)$$
15

- Using these coordinates, we proceed as we did in 3.4 and 3.5: we generate  $S_k$  and  $S_{kt}$  matrices,
- 619 use them to correct the data and to identify the data point with the smallest error for each
- crossing cycle. We report the time, error estimate, and corrected height for the minimum-error
- datapoint from each cycle, as well as the location, pair, and track number corresponding to the
- datum point in the /ptx/crossing track data group. Because the crossing angles between the
- tracks are oblique at high latitudes, a particular crossing track may appear in a few subsequent
- datum points; in these cases, we expect that the error estimates should vary with the distance

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- between the crossing track and the datum track, so that the point with the minimum error should
- 626 correspond to the precise crossing location of the two tracks.
- To help evaluate the quality of crossing-track data we calculate the *along track rss* parameter
- for each crossing-track measurement. This parameter gives the RSS of the differences between
- each segment's endpoint heights and the heights of the previous and subsequent segments. A
- segment that is consistent with the previous and next segments in slope and elevation will have a
- small value for this parameter, a segment that is inconsistent (and thus potentially in error) will
- have a large value. Crossing-track measurements that have values greater than 10 m are
- excluded form ATL11 and do not appear in the dataset.

## 3.7 Calculating parameter averages

- ATL11 contains a variety of parameters that mirror parameters in ATL06, but are averaged to the
- 636 140-m ATL11 resolution. Except where noted otherwise, these quantities are weighted averages
- of the corresponding ATL06 values. For selected pairs (i.e. those included in the reference-
- surface fit), the parameters are averaged over the selected segments from each cycle, using
- weights derived from their formal errors, h li sigma. The parameter weighted average for the  $N_k$
- segments from cycle k is then:

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$$\langle q \rangle = \frac{\sum_{i=1}^{N_k} |\sigma_i^{-2}| q_i}{\sum_{i=1}^{N_k} |\sigma_i^{-2}|}$$
 16

- Here  $q_i$  are the parameter values for the segments. For repeats with no selected pairs, recall that
- the corrected height for only one segment is reported in /ptx/h corr; for these, we simply report
- the corresponding parameter values for that selected segment.

#### 3.8 Output data editing

The output data product includes cycle height estimates only for those cycles that have non-systematic error estimates (/ptx/h\_corr\_sigma) less than 15 m. All other heights (and their errors) are reported as *invalid*.

#### 4.0 LAND ICE PRODUCTS: LAND ICE H (T)(ATL 11/L3B)

- Each ATL11 file contains data for a single reference ground track, for one of the subregions
- defined for ATLAS granules (see Figure 6-3). The ATL11 consists of three top-level groups, one
- for each beam pair (pt1, pt2, pt3). Within each pair-track group, there are datasets that give the
- corrected heights for each cycle, their errors, and the reference-point locations. Subgroups
- 656 (cycle stats, and ref surf) provide a set of data-quality parameters, and ancillary data describing
- 657 the fitting process, and use the same ordering and coordinates as the top-level group (i.e. any
- dataset within the /ptx/cycle stats and /ptx/ref surf groups refers to the same latitude, longitude,
- and reference points as the corresponding measurements in the /ptx/ groups.) The
- 660 crossing track data group gives height measurements at crossover locations, and has its own set
- of locations and

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## 4.1.1 File naming convention

- ATL11 files are named in the following format:
- ATL11\_ttttgg\_cccc\_rrr\_vv.h5
- Here tttt is the rgt number, gg is the granule-region number, cccc gives the first and last cycles of
- along-track data included in the file (e.g. 0308 would indicate that cycles three through eight,
- inclusive, might be included in the along-track solution), and rrr is the release number. and vv is
- the version number, which is set to one the first time a granule is generated for a given data
- release, and is incremented by one if the granule is regenerated.

- 672 **4.2** /ptx group
- **673 4.3**
- shows the datasets in the ptx groups. This group gives the principal output parameters of the
- ATL11. The corrected repeat measurements are in /ptx/h corr, which gives improved height
- 676 measurements based on a surface fit to valid data at paired segments. The associated reference
- 677 coordinates, /ptx/latitude and /ptx/longitude give the reference point location, with averaged
- times per repeat, /ptx/delta time. For repeats with no selected pairs, the corrected height is that
- from the selected segment with the lowest error. Two error metrics are given in
- 680 /ptx/h corr sigma and /ptx/h corr sigma systematic. The first gives the error component due to
- ATL06 range errors and due to uncertainty in the reference surface. The second gives the
- component due to geolocation and radial-orbit errors that are correlated at scales larger than one
- reference point; adding these values in quadrature gives the total per-cycle error. Values are only
- 684 reported for /ptx/h corr, /ptx/h corr sigma, and /ptx/h corr sigma systematic for those cycles
- whose uncorrelated errors are less than 15 m; all others are reported as *invalid*. A
- 686 /ptx/quality summary is included for each cycle, based on fit statistics from ATL06.

Table 4-1 Parameters in the /ptx/ group

Parameter	Units	Dimensions	Description
cycle_number	counts	$1xN_{cycles}$	Cycle number for each column of the data
latitude	degrees North	$N_{pts}  imes 1$	Reference point latitude
longitude	degrees East	$N_{pts} \times 1$	Reference point longitude
ref_pt	counts	$N_{pts}{ imes}1$	The reference point number, $m$ , counted from the equator crossing of the RGT.
delta_time	seconds	$N_{pts} \!\!  imes N_{cycles}$	mean GPS time for the segments for each cycle
h_corr	meters	$N_{pts} \times N_{cycles}$	the mean corrected height
h_corr_sigma	meters	$N_{pts}  imes N_{cycles}$	the formal error in the corrected height
h_corr_sigma_systematic	meters	$N_{pts} \!\!  imes N_{cycles}$	the magnitude of the RSS of all errors that might be correlated at scales larger than a single reference point (e.g. pointing errors, GPS errors, etc)
quality_summary	counts	$N_{pts} \!\!  imes N_{cycles}$	summary flag: zero indicates high-quality cycles: where min(signal_selection_source)<=1 and min(SNR_significance) < 0.02, and ATL06_summary_zero_count >0.

#### 4.4 /ptx/ref surf group

Table 4-2 describes the /ptx/ref\_surf group. This group includes parameters describing the reference surface fit at each reference point. The polynomial coefficients are given in /ptx/poly\_ref\_surf, sorted first by total degree, then by x-component degree. Because the polynomial degree is chosen separately for each reference point, enough columns are provided in the /ptx/poly\_ref\_surf and /ptx/poly\_ref\_surf\_sigma to accommodate all possible components up to 2<sup>rd</sup> degree in y and 3<sup>th</sup> degree in x, and absent values are filled in with zeros. The correspondence between the columns of the polynomial fields and the exponents of the x and y terms are given in the /ptx/poly\_exponent\_x and /ptx/poly\_exponent\_y fields. The time origin for the slope change is given in the group attribute /ptx/slope\_change\_t0.

Table 4-2 Parameters in the /ptx/ref surf group

Parameter	Units	Dimensions	Description
complex_surface_flag	counts	$N_{pts}  imes I$	0 indicates that normal fitting was attempted, 1 indicates that the signal selection algorithm rejected too many repeats, and only a linear fit was attempted
rms_slope_fit	counts	$N_{pts} \times I$	the RMS of the slope of the fit polynomial within 50 m of the reference point
e_slope	counts	$N_{pts} \times I$	the mean East-component slope for the reference surface within 50 m of the reference point
n_slope	counts	$N_{pts} \times I$	the mean North-component slope for the reference surface within 50 m of the reference point
at_slope	Counts	$N_{pts} \times I$	Mean along-track component of the slope of the reference surface within 50 m of the reference point
xt_slope		$N_{pts} \times I$	Mean across-track component of the slope of the reference surface within 50 m of the reference point
deg_x	counts	$N_{pts} \times I$	Maximum degree of non-zero polynomial components in x
deg_y	counts	$N_{pts} \times I$	Maximum degree of non-zero polynomial components in y

poly_exponent_x	counts	1x8	Exponents for the x factors in the surface polynomial
poly_exponent_y	counts	1x8	Exponents for the y factors in the surface polynomial
poly_coeffs	counts	$N_{pts} \times 8$	polynomial coefficients (up to degree 3), for polynomial components scaled by 100 m
poly_ref_coeffs_sigma	counts	$N_{pts} \times 8$	formal errors for the polynomial coefficients
ref_pt_number	counts	$N_{pts} \times I$	Ref point number, counted from the equator crossing along the RGT.
x_atc	meters	$N_{pts}  imes 1$	Along-track coordinate of the reference point, measured along the RGT from its first equator crossing.
y_atc	meters	$N_{pts}  imes I$	Across-track coordinate of the reference point, measured along the RGT from its first equator crossing.
rgt_azimuth	degrees	$N_{pts}  imes 1$	Reference track azimuth, in degrees east of local north
slope_change_rate_x	years-1	$N_{pts} \times I$	rate of change of the x component of the surface slope
slope_change_rate_y	years <sup>-1</sup>	$N_{pts} \times 1$	rate of change of the y component of the surface slope
slope_change_rate_x_sigma	years-1	$N_{pts}  imes I$	Formal error in the rate of change of the x component of the surface slope
slope_change_rate_y_sigma	years-1	$N_{pts} \times I$	Formal error in the rate of change of the y component of the surface slope
misfit_chi2r	meters	$N_{pts}  imes I$	misfit chi square, divided by the number of degrees in the solution
misfit_rms	meters	$N_{pts}  imes I$	RMS misfit for the surface-polynomial fit
fit_quality	counts	$N_{pts} \times I$	Indicates quality of the fit:

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0: no problem identified
1: One or more polynomial coefficient errors larger than 2
2: One or more components of the surface slope has magnitude larger than 0.2
3: Conditions 1 and 2 both true.

The slope of the fit surface is given in the ref\_surf/n\_slope and ref\_surf/e\_slope parameters in the local north and east directions; the corresponding slopes in the along-track and across-track directions are given in the ref\_surf/xt\_slope and ref\_surf/yt\_slope parameters. For the along-track points, the surface slope is calculated by evaluating the correction-surface polynomial for a 10-m spaced grid of points extending ±50 m in x and y around the reference point, and calculating the mean slopes of these points. The calculation is performed in along-track coordinates and then projected onto the local north and east vectors. The rms\_slope\_fit is derived from the same set of points, and is calculated as the RMS of the standard deviations of the slopes calculated from adjacent grid points, in x and y.

#### 4.5 /ptx/cycle stats group

- 713 The /ptx/cycle\_stats group gives summary information about the segments present for each reference point. Most parameters are averaged according to equation 14, but for others (e.g.
- 715 /ptx/signal selection flag best, which is the minimum of the signal selection flags for the cycle)
- **Table 4-3** describes how the summary statistics are derived.

Table 4-3 Parameters in the /ptx/cycle stats group

Parameter	Units	Dimensions	Description
ATL06_summary_zero_count	counts		Number of segments with atl06_quality_summary=0 (0 indicates the best-quality data)
h_rms_misfit	meters	$N_{pts} \times N_{cycles}$	Weighted-average RMS misfit between PE heights and along-track land-ice segment fit
r_eff	counts		Weighted-average effective, uncorrected reflectance for each cycle.

Parameter	Units	Dimensions	Description
tide_ocean	meters	$N_{pts} \times N_{cycles}$	Weighted-average ocean tide for each cycle
dac	meters	$N_{pts} \times N_{cycles}$	Dynamic atmosphere correction (mainly the effect of atmospheric pressure on floating-ice elevation).
cloud_flg_atm	counts	$N_{pts} \times N_{cycles}$	Minimum cloud flag from ATL06: Flag indicates confidence that clouds with OT* > 0.2 are present in the lower 3 km of the atmosphere based on ATL09
cloud_flg_asr	counts	$N_{pts}  imes N_{cycles}$	Minimum apparent-surface-reflectance - based cloud flag from ATL06: Flag indicates confidence that clouds with OT > 0.2 are present in the lower 3 km of the atmosphere based on ATL09
bsnow_h	meters	$N_{pts} \times N_{cycles}$	Weighted-average blowing snow layer height for each cycle
bsnow_conf	counts	$N_{pts} \!\!  imes N_{cycles}$	Maximum bsnow_conf flag from ATL06: indicates the greatest (among segments) confidence flag for presence of blowing snow for each cycle
x_atc	meters	$N_{pts} \times N_{cycles}$	weighted average of pair-center RGT y coordinates for each cycle
y_atc	meters	$N_{pts} \times N_{cycles}$	weighted mean of pair-center RGT y coordinates for each cycle
ref_pt		$N_{pts} \times N_{cycles}$	Ref point number, counted from the equator crossing along the RGT.
seg_count	counts	$N_{pts} \!\!  imes N_{cycles}$	Number of segments marked as valid for each cycle. Equal to 0 for those cycles not included in the reference-surface shape fit.
min_signal_selection_source	counts	$N_{pts} \!\!  imes N_{cycles}$	Minimum of the ATL06 signal_selection_source value (indicates the highest-quality segment in the cycle)
min_snr_significance	counts	$N_{pts} \times N_{cycles}$	Minimum of SNR_significance (indicates the quality of the best segment in the cycle)

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Parameter	Units	Dimensions	Description
sigma_geo_h	meters	$N_{pts} \times N_{cycles}$	Root-mean-weighted-square-average total vertical geolocation error due to PPD and POD
sigma_geo_at	meters	$N_{pts} \times N_{cycles}$	Root-mean-weighted-square- average local-coordinate x horizontal geolocation error for each cycle due to PPD and POD
sigma_geo_xt	meters	$N_{pts} \times N_{cycles}$	Root-mean-weighted-square- average local-coordinate y horizontal geolocation error for each cycle due to PPD and POD
h_mean	meters	$N_{pts} \times N_{cycles}$	Weighted-average of surface heights, not including the correction for the reference surface

\*OT (optical thickness) is a measure of signal attenuation used in atmospheric calculations. This parameter discussed in ICESat-2 atmospheric products (ATL09)

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#### 4.6 /ptx/crossing track data group

The /ptx/crossing track data group (Table 4-4) contains elevation data at crossover locations. These are locations where two ICESat-2 pair tracks cross, so data are available from both the datum track, for which the granule was generated, and from the crossing track. The data in this group represent the elevations and times from the crossing tracks, corrected using the reference surface from the datum track. Each set of values gives the data from a single segment on the crossing track, that was selected as having the minimum error among all segments on the crossing track within the 2 L search XT-by-2 L search AT window around the reference point on the datum track. The systematic errors are evaluated based on the magnitude of the reference-

731 surface slope and the magnitude of the horizontal geolocation error of the crossing-track data. 732

Attributes for the group specify the track number and pair-track number of the crossing track.

Table 4-4 Parameters in the /ptx/crossing track data group

Parameter	Units	Dimensions	Description
ref_pt	counts	$N_{XO} \times 1$	the reference-point number for the datum track
delta_time	years	N <sub>XO</sub> × 1	time relative to the ICESat-2 reference epoch

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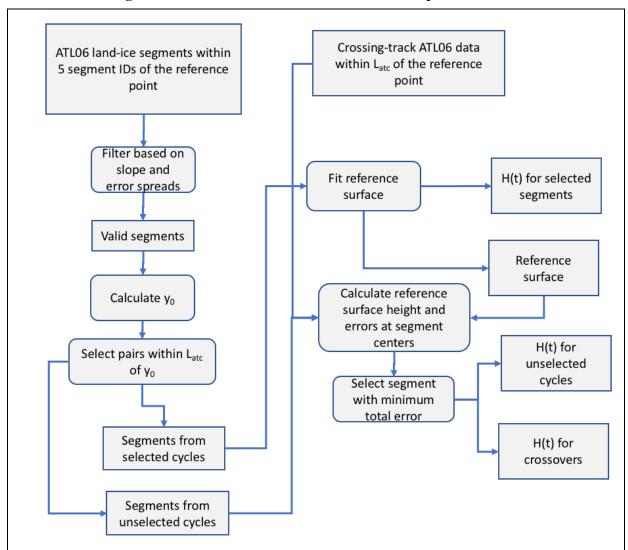
h_corr	meters	$N_{XO} \times 1$	WGS-84 height, corrected for the ATL11 surface shape
h_corr_sigma	meters	$N_{XO} \times 1$	error in the height estimate
h_corr_sigma_systematic	meters	$N_{XO} \times 1$	systematic error in the height estimate
ocean_tide	Meters	$N_{XO} \times 1$	Ocean-tide estimate for the crossing track
dac	Meters	$N_{XO} \times 1$	Dynamic atmosphere correction for the crossing track
latitude	degrees	$N_{XO} \times I$	latitude of the crossover point
longitude	degrees	$N_{XO} \times 1$	longitude of the crossover point
cycle_number	counts	$N_{XO} \times 1$	Cycle number for the crossing data
rgt	counts	N <sub>XO</sub> × 1	The RGT number for the crossing data
spot_crossing	counts	N <sub>XO</sub> × 1	The spot number for the crossing data
atl06_quality_summary	counts	N <sub>XO</sub> × I	quality flag for the crossing data derived from ATL06. 0 indicates no problems detected, 1 indicates potential problems
along_track_rss	meters	$N_{XO} \times I$	Root sum of the squared differences between the heights of the endpoints for the crossing- track segment and the centers of the previous and next segments

#### 5.0 ALGORITHM IMPLEMENTATION

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Figure 5-1 Flow Chart for ATL11 Surface-shape Corrections



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741 The following steps are performed for each along-track reference point.

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1. Segments with *segment\_id* within *N\_search/2* of the reference-point number, are selected.

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2. Valid segments are identified based on estimated errors, the *ATL06\_quality\_summary* parameter, and the along- and across-track segment slopes. Valid pairs, containing valid measurements from two different beams, are also identified.

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- 747 3. The location of the reference point is adjusted to allow the maximum number of repeats 748 with at least one valid pair to fall within the across-track search distance of the reference 749 point.
  - 4. The reference surface is fit to pairs with two valid measurements within the search distance of the reference point. This calculation also produces corrected heights for the selected pairs and the errors in the correction polynomial coefficients.
  - 5. The correction surface is used to derive corrected heights for segments not selected in steps 1-3, and the height for the segment with the smallest error is selected for each
  - 6. The reference surface is used to calculate heights for external (pre-ICESat-2) laser altimetry data sets and crossover ICESat-2 data.
- 757 A schematic of this calculation is shown in Figure 5-1.

### 5.1.1 Select ATL06 data for the current reference point

**759 Inputs:** 

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- 760 ref pt: segment number for the current reference point
- 761 track num: The track number for current point
- 762 pair num: The pair number for the current point
- 763 **Outputs:**
- 764 D ATL06: ATL06 data structure
- 765 **Parameters:**
- 766 N search: number of segments to search, around ref. pt, equal to 5.
- 767 Algorithm:
- 768 1. For each along-track point, load all ATL06 data from track track num and pair pair num that
- have segment id within N search of ref pt: These segments have ref pt N search
- 770 <= segment id <= ref pt +N search.
- 2. Reject any data that have y atc values more than 500 m distant from the nominal pair-track
- 772 centers (3200 m for pair 1, 0 m for pair 2, -3200 m for pair 3).

#### 774 5.1.2 Select pairs for the reference-surface calculation

775 Inputs:

- 776 ref pt: reference point number for the current fit
- 777 x atc ctr: Along-track coordinate of the reference point
- 778 D ATL06: ATL06 data structure
- 779 pair data: Structure describing ATL06 pairs, includes mean of strong/weak beam y atc and
- 780 *dh fit dy*

781 **Outputs:** 782 validity flags for each segment: 783 valid segs.x slope: Segments identified as valid based on x-slope consistency 784 valid segs.data: Segments identified as valid based on ATL06 parameter values. 785 Validity flags for each pair: 786 valid pairs: Pairs selected for the reference-surface calculation 787 valid pairs.y slope: Pairs identified as valid based on y-slope consistency 788 y polyfit ctr: y center of the slope regression 789 ref surf/complex surface flag: Flag indicating 0: non-complex surface, 1: complex surface. 790 791 **Parameters:** 792 L search XT: The across-track search distance. 793 N search: Along-track segment search distance 794 seg sigma threshold min: Minimum threshold for accepting errors in segment heights, equal to 795 0.05 m. 796 Algorithm: 797 1. Flag valid segments based on ATL06 values. 798 1a. Count the cycles that contain at least one pair that has at 106 quality flag=0 799 for both segments. If this number is greater than N cycles/3, set 800 ref surf/complex surface flag=0 and set valid segs.data to 1 for segments with ATL06 quality summary equal to 0. Otherwise, set ref surf/complex surface flag=1 and set 801 802 valid segs.data to 1 for segments with snr significance < 0.02. 803 1b. Define seg sigma threshold as the maximum of 0.05 or three times the median of 804 sigma h li for segments with valid segs.data equal to 1. Set valid segs.data to 1 for segments 805 with h sigma li less than this threshold and ATL06 quality summary equal to 0. 806 1c. Define valid pairs.data: For each pair of segments, set valid pairs.data to 1 when 807 both segments are marked as valid in valid segs.data. 808 2. Calculate representative values for the x and y coordinate for each pair, and filter by distance. 809 2a. For each pair containing two defined values, set pair datax to the segments' x atc 810 value, and pair data.y to the mean of the segments' y atc values. 811 2b. Calculate y polyfit ctr, equal to the median of pair data y for pairs marked valid in valid pairs.data. 812 813

2c. Set valid pairs. ysearch to 1 for pairs with |pair data.y - y polyfit ctr| <

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L search XT.

3. Select pairs based on across-track slope consistency

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- 3a. Define *pairs\_valid\_for\_y\_fit*, for the across-track slope regression if they are marked as valid in *valid pairs.data*, and *valid pairs.ysearch*, not otherwise.
  - 3b. Choose the degree of the regression for across-track slope
- -If the valid pairs contain at least two different *x\_atc* values (separated by at least 820 18 m), set the along-track degree, *my regression y degree*, to 1, 0 otherwise.
- -If valid pairs contain at least two different *ref\_surf/y\_atc* values (separated by at least 18 m), set the across-track degree, *my regression y degree*, to 1, 0 otherwise.
  - 3c. Calculate the formal error in the y slope estimates:  $y\_slope\_sigma$  is the RSS of the  $h\_li\_sigma$  values for the two beams in the pair divided by the difference in their  $y\_atc$  values. Based on these, calculate  $my\_regression\_tol$ , equal to the maximum of 0.01 or three times the median of  $y\_slope\_sigma$  for valid pairs (pairs valid for  $y\_fit$ ).
  - 3d. Calculate the regression of *dh\_fit\_dy* against *pair\_data.x* and *pair\_data.y* for valid pairs (*pairs\_valid\_for\_y\_fit*). The result is *y\_slope\_model*, which gives the variation of *dh\_fit\_dy* as a function of *x\_atc* and *y\_atc*. Calculate *y\_slope\_resid*, the residuals between the *dh\_fit\_dy* values and *y\_slope\_model* for all pairs in *pair\_data*.
- 3e. Calculate *y\_slope\_threshold*, equal to the maximum of *my\_regresion\_tol* and three times the RDE of *y\_slope\_resid* for valid pairs.
- 3f. Mark all pairs with |*y\_slope\_resid*| > *y\_slope\_threshold* as invalid. Re-establish pairs\_valid\_for\_y\_fit (based on valid\_pairs.data, valid\_pairs.y\_slope and valid\_pairs.ysearch).

  Return to step 3d (allow two iterations total).
  - 3g. After the second repetition of 3d-f, use the model to mark all pairs with |y slope resid| less than y\_slope threshold with 1 in valid pairs.y slope, 0 otherwise.
- 4. Select segments based on along-track slope consistency for both segments in the pair
  - 4a. Define *pairs\_valid\_for\_x\_fit*, valid segments for the along-track slope regression: segments are valid if they come from pairs marked as valid in *valid\_pairs.data* and *valid\_pairs.vsearch*, not otherwise.
    - 4b. Choose the degree of the regression for along-track slope
  - -If valid segments contain at least two different  $x\_atc$  values set the along-track degree, mx regression x degree, to 1, 0 otherwise.
  - -If valid segments contain at least two different *y\_atc* values, set the across-track degree, *mx\_regression\_y\_degree*, to 1, 0 otherwise.
  - 4c. Calculate along-track slope regression tolerance,  $mx\_regression\_tol$ , equal to the maximum of either 0.01 or three times the median of the  $dh\_fit\_dx\_sigma$  values for the valid pairs.
- 4d. Calculate the regression of *dh\_fit\_dx* against *pair\_data.x* and *pair\_data.y* for valid segments (*pairs valid for x fit*). The result is *x slope model*, which gives the variation of

- 852 dh\_fit\_dx as a function of pair\_data.x and pair\_data.y. Calculate x\_slope\_resid, the residuals
  853 between the dh\_fit\_dx and x\_slope\_resid for all segments for this reference point, seg\_x\_center
  854 and y polyfit ctr.
- 4e. Calculate *x\_slope\_threshold*, equal to the maximum of either *mx\_regression\_tol* or three times the RDE of *x slope resid* for valid segments.
- 4f. Mark *valid\_segs.x\_slope* with |*x\_slope\_resid*| > *x\_slope\_threshold* as invalid. Reestablish *valid\_pairs.x\_slope* when both *valid\_segs.x\_slope* equal 1. Re-establish pairs\_valid\_for\_x\_fit. Return to step 4d (allow two iterations total).
  - 4g. After the second repetition of 4d-f, mark all segments with |x\_slope\_resid| less than x\_slope\_threshold with 1 in seg\_valid\_xslope, 0 otherwise. Define valid\_pairs.x\_slope as 1 for pairs that contain two segments with valid\_segs.x\_slope=1, 0 otherwise.
  - 5. Re-establish *valid\_pairs.all*. Set equal to 1 if *valid\_pairs.x\_slope*, *valid\_pairs.y\_slope*, and *valid\_pairs.data* are all valid.
- 5a. Identify *unselected cycle segs*, as those *D6.cycles* where *valid pairs.all* are False.

# 5.1.3 Adjust the reference-point y locaction to include the maximum number of cycles

**869 Inputs:** 

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- 870  $D_ATL06$ : ATL06 structure for the current reference point.
- 871 *valid pairs:* Pairs selected based on parameter values and along- and across-track slopes.
- 872 **Outputs:**
- 873 ref surf/y atc: Adjusted fit-point center y.
- 874 *valid pairs*: validity masks for pairs, updated to include those identified as valid based on the
- spatial search around y atc ctr.
- 876 **Parameters**:
- 877 L search XT: Across-track search length (equal to 110 m)
- 878 **Algorithm:**
- 1. Define  $y\theta$  as the median of the unique integer values of the pair center y\_atc for all valid pairs. Set a range of y values,  $y\theta$  shifts, as round( $y\theta$ ) +/- 100 meters in 2-meter increments.
- 2. For each value of y0\_shifts (y0\_shift), set a counter, selected\_seg\_cycle\_count, to the number of distinct cycles for which both segments of the pair are contained entirely within the y interval [y0\_shift- L\_search\_XT, y0\_shift+ L\_search\_XT]. Add to this, the number of distinct cycles represented by unpaired segments contained within that interval, weighted by 0.01. The sum is called score.

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- 3. Search for an optimal y-center value (with the most distinct cycles). Set y\_best to the value of y0\_shift that maximizes score. If there are multiple y0\_shift values with the same, maximum score, set to the median of the v0\_shift values with the maximum score.
- 4. Update *valid\_pairs* to include all pairs with *y\_atc* within +/- L\_search\_XT from *y atc ctr*.

#### 5.1.4 Calculate the reference surface and corrected heights for selected pairs

892 Inputs:

- 893 D ATL06: ATL06 structure for the current reference point, containing parameters for each
- 894 segment:
- 895 *x atc*: along-track coordinate
- 896 *y atc*: across-track coordinate
- 897 *delta t:* time for the segment
- 898 pair data: Structure containing information about ATL06 pairs. Must include:
- 899 *y atc:* Pair-center across-track coordinates
- 900 *valid pairs*: Pairs selected based on parameter values and along- and across-track slope.
- 901 x atc ctr: The reference point along-track x coordinate (equal to ref surf/x atc).
- 902 *y atc ctr*: The reference point along-track x coordinate (equal to *ref surf/y atc*)
- 903 **Outputs:**
- 904 ref surf/deg x: Degree of the reference-surface polynomial in the along-track direction
- 905 ref surf/deg y: Degree of the reference-surface polynomial in the across-track direction
- 906 ref surf/poly coeffs: Polynomial coefficients of the reference-surface fit
- 907 ref surf/poly coeffs sigma: Formal error in polynomial coefficients of the reference-surface fit
- 908 ref surf/slope change rate x: Rate of change of the x component of the surface slope
- 909 ref surf/slope change rate x sigma: Formal error in the rate of change of the x component of
- 910 the surface slope
- 911 ref surf/slope change rate y: Rate of change of the y component of the surface slope
- 912 ref surf/slope change rate y sigma: Formal error in the rate of change of the y component of
- 913 the surface slope
- 914 r seg: Segment residuals from the reference-surface model
- 915 /ptx/h corr: Partially filled-in per-cycle corrected height for cycles used in reference surface
- 916 /ptx/h corr sigma: Partially filled-in per-cycle formal error in corrected height for cycles used in
- 917 reference surface
- 918 ref surf cycles: A list of cycles used in defining the reference surface

- 919 *C m surf*: Covariance matrix for the reference-polynomial and surface-change model
- 920 fit columns surf: Mask identifying which components of the combined reference-polynomial
- and surface-change model were included in the fit.
- 922 degree list x: The x degrees corresponding to the columns of matrix used in fitting the reference
- 923 surface to the data
- 924 degree list y: The y degrees corresponding to the columns of matrix used in fitting the reference
- 925 surface to the data
- 926 selected segments: A set of flags indicating which segments were selected by the iterative
- 927 fitting process.
- Partially filled-n per-cycle ATL11 output variables (see table 4-3) for cycles used in reference
- 929 surface
- 930 Parameters:
- 931 poly max degree AT: Maximum polynomial degree for the along-track fit, equal to 3.
- 932 poly max degree XT: Maximum polynomial degree for the across-track fit, equal to 2.
- 933 slope change t0: Half the duration of the mission (equal to the time of the last-possible
- elevation value minus the time of the start of data collection, divided by two).
- 935 max fit iterations: Maximum number of iterations for surface fitting, with acceptable residuals,
- 936 equal to 20.
- 937 xy scale: The horizontal scaling value used in polynomial fits, equal to 100 m
- 938 t scale: The time scale used in polynomial fits, equal to seconds in 1 year.
- 939 **Algorithm**:

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- 1. Build the cycle design matrix: **G\_zp** is a matrix that has one column for each distinct cycle in *selected\_pairs* and one row for each segment whose pair is in *selected pairs*. For each segment, the corresponding row of **G\_zp** is 1 for the column matching the cycle for that segment and zero otherwise.
  - 2. Select the polynomial degree.

The degree of the x polynomial, ref\_surf/deg\_x, is: min(poly\_max\_degree\_AT, maximum(number of distinct values of round((x\_atc-x\_atc\_ctr)/20) among the selected segments in any one cycle) -1), and the degree of the y polynomial, ref\_surf/deg\_y, is: min(poly\_max\_degree\_XT, number of distinct values of round((pair\_data.y\_atc-y\_atc\_ctr)/20) among the selected pairs)

- 3. Perform an iterative fit for the reference-surface polynomial.
- 3a. Define degree\_list\_x and degree\_list\_y: This array defines the x and y degree of the polynomial coefficients in the polynomial surface model. There is one component for each unique degree combination of x degrees between 0 and ref\_surf/deg\_x and for y degree between 0 and ref\_surf/deg\_y such that x degree + y degree <= max(ref\_surf/deg\_x, ref\_surf/deg\_y),

except that there is no  $x\_degree=0$  and  $y\_degree=0$  combination. They are sorted first by the sum of the x and y degrees, then by x degree, then by y degree.

- 3b. Define the polynomial fit matrix. **S\_fit\_poly** has one column for each element of the polynomial degree arrays, with values equal to  $((x\_atc x\_atc\_ctr)/xy\_scale)^{x\_degree}$  ( $(y\_atc-y\_atc\_ctr)/xy\_scale)^{y\_degree}$ . There is one row in the matrix for every segment marked as *selected*.
- 3c. If the time span is longer than 1.5 years, define slope-change matrices, **S\_fit\_slope\_change**. The first column of the matrix gives the rate of slope change in the x component, equal to  $(x\_atc-x\_atc\_ctr)/xy\_scale*(delta\_time-slope\_change\_t0)/t\_scale$ . The second column gives the rate of slope change in the y component, equal to  $(y\_atc-y\_atc\_ctr)/xy\_scale*(delta\_time-slope\_change\_t0)/t\_scale$ .
- 3d. Build the surface matrix, **G\_surf**, and the combined surface and cycle-height matrix, **G\_surf\_zp**: The surface matrix is equal to the horizontal catenation of **S\_fit\_poly**, and, if defined, **S\_fit\_slope\_change**. The combined surface and cycle-height matrix, **G\_surf\_zp**, is equal to the horizontal catenation of **G\_surf** and **G\_zp**.
- 3e. Subset the fitting matrix. Subset  $G_{surf}$  by row to include only rows corresponding to selected segments to produce G (on the first iteration, all are *selected*). Next, subset G by column, first to eliminate all-zero columns, and second to include only columns that are linearly independent from one another: calculate the normalized correlation between each pair of columns in G, and if the correlation is equal to unity, eliminate the column with the higher weighted degree ( $poly_{wt}$  sum =  $x_{degree}$  + 1.1\* $y_{degree}$ , with the factor of 1.1 chosen to avoid ties). Identify the selected columns in the matrix as  $fit_{columns}$ . If more than three of the original surface-change columns have been eliminated, set the  $ref_{surf}$ /complex\_surface\_flag to True, mark all columns corresponding to polynomial coefficients of combined x and y degree greater than 1 as False in  $fit_{surf}$  columns.
- 3f. Check whether the inverse problem is under- or even-determined: If the number of selected\_segments is less than the number of columns of **G**, eliminate remaining columns of **G** in descending order of poly\_wt\_sum until the number of columns of **G** is less than the number of selected segments.
- 3g. Generate the data-covariance matrix,  $\mathbf{C}_{-}\mathbf{d}$ . The data-covariance matrix is a square matrix whose diagonal elements are the squares of the  $h_{li\_sigma}$  values for the selected segments.
- 3h. Calculate the polynomial fit. Initialize *m\_surf\_zp*, the reference model, to a vector of zero values, with one value for each column of **G\_surf\_zp**. Calculate the generalized inverse (equation 7), of **G**, **G\_g**. If the inversion calculation returns an error, or if any row of **G\_g** is all-zero (indicating some parameters are not linearly independent), report fit failure and return. Otherwise, multiply **G\_g** by the subset of *h\_li* corresponding to the selected segment to give *m*, containing values for the parameters selected in *fit\_columns*. Fill in the components of *m\_surf\_zp* flagged in *fit\_columns* with the values in *m*.
- 3i. Calculate model residuals for all segments,  $r\_seg$ , equal to  $h\_li$ - $G\_surf\_dz$  \*  $m\_surf\_zp$ . The subset of  $r\_seg$  corresponding to selected segments is  $r\_fit$ .

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- 3j. Calculate the fitting tolerance,  $r\_tol$ , equal to three times the RDE of the  $r\_fit/h\_li\_sigma$  for all selected segments. Calculate the reduced chi-squared value for these residuals,  $ref\_surf/misfit\_chi2$ , equal to  $r\_fit^TC\_d^{-1}r\_fit$ . Calculate the P value for the misfit, equal to one minus the CDF of a chi-squared distribution with m-n degrees of freedom for  $ref\_surf/misfit\_chi2$ , where m is the number of rows in G, and n is the number of columns.
- 3k. If the *P* value is less than 0.025 and fewer than  $max\_fit\_iterations$  have taken place, mark all segments for which  $|r\_seg/h\_li\_sigma| < r\_tol$  as selected, and return to 3e. Otherwise, continue to 3k.
- 31. Propagate the errors. Based on the most recent value of  $\mathbf{C}_{-}\mathbf{d}$ , generate a revised data-covariance matrix,  $\mathbf{C}_{-}\mathbf{dp}$ , whose diagonals values are the maximum of  $h_{-}li_{-}sigma^{2}$  and RDE $(r_{-}fit)^{2}$ . Calculate the model covariance matrix,  $\mathbf{C}_{-}\mathbf{m}$  using equation 9. If any of the diagonal elements of  $\mathbf{C}_{-}\mathbf{m}$  are larger than  $10^{4}$ , report a fit failure and return. Fill in elements of  $m_{-}surf_{-}zp$  that are marked as valid in  $fit_{-}columns$  with the square roots of the corresponding diagonal elements of  $\mathbf{C}_{-}\mathbf{m}$ . If any of the errors in the polynomial coefficients are larger than 2, set  $ref_{-}surf_{-}fit_{-}quality=1$ .
- 1010 4. Return a list of cycles used in determining the reference surface in *ref\_surf\_cycles*. These
- 1011 cycles have columns in G that contain a valid pair, and for which the steps 3e and 3j did not
- eliminate the degree of freedom. For these cycles, partially fill in the values of /ptx/h\_corr and
- 1013 /ptx/h\_corr\_sigma, from **m** and **m\_sigma**. Similarly, fill in values for
- 1014 /ptx/h\_corr\_sigma\_systematic (Equation 12) and /ptx/delta\_time, as well as all variables in Table
- 4-3. Set /ptx/h\_corr, /ptx/h\_corr\_sigma, /ptx/h\_corr\_sigma\_systematic to NaN for those cycles
- that have uncorrelated error estimates greater than 15 m.
- Values from Table 4-2 defining the fitted reference surface are also reported including
- 1018 ref surf/poly coeffs, and ref surf/poly coeffs sigma, ref surf/slope change rate x,
- 1019 ref surf/slope change rate y, ref surf/slope change rate x sigma, and
- 1020 ref\_surf/slope\_change\_rate\_y\_sigma.
- Return **C\_m\_surf**, the portion of **C\_m** corresponding to the polynomial and slope-change
- components of C\_m. Return selected\_cols\_surf, the subset of selected\_cols corresponding to the
- surface polynomial and slope-change parameters.
- Return the reduced chi-square value for the last iteration, ref surf/misfit chi2r, equal to
- 1025 ref\_surf/misfit\_chi2/(m-n).
- 1027 5.1.5 Calculate corrected heights for cycles with no selected pairs.
- **1028 Inputs:**

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- 1029 **C\_m\_surf**: Covariance matrix for the reference-surface model.
- 1030 degree\_list\_x, degree\_list\_y: List of x-, y-, degrees for which the reference-surface calculation
- attempted an estimate.

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- selected cols surf: Parameters of the combined reference-surface and slope-change model for
- which the inversion returned a value. There should be one value for each row/column of
- 1034 C m surf.
- 1035 x atc ctr, y atc ctr: Center point for the surface fit (equal to ref surf/x atc, ref surf/y atc)
- selected segments: Boolean array indicating segments selected for the reference-surface
- 1037 calculation
- 1038 valid segs.x slope: Segments identified as valid based on x-slope consistency
- 1039 *valid segs.data*: Segments identified as valid based on ATL06 parameter values.
- 1040 pair\_number: Pair number for each segment
- 1041 *h li*: Land-ice height for each segment
- 1042 *h li sigma*: Formal error in *h li*.
- 1043 /ptx/h corr: Partially filled-in per-cycle corrected height
- 1044 /ptx/h corr sigma: Partially filled-in per-cycle corrected height error
- 1045 ref surf/poly coeffs: Polynomial coefficients from 2-d reference-surface fit
- 1046 ref surf cycles: A list of cycles used in defining the reference surface
- 1047 ref surf/slope change rate x, ref surf/slope change rate y: Rate of change of the x and y
- 1048 components of the surface slope
- 1049 ref surf/N slope, ref surf/E slope: slope components of reference surface
- 1050 sigma geo r: Radial component of the geologation error for the crossing track
- 1051 D ATL06: ATL06 data structure
- Partially filled-in per-cycle ATL11 output variables (see table 4-3)
- 1053 **Outputs:**
- 1054 /ptx/h corr: Per-cycle corrected height
- 1055 /ptx/h corr sigma: Per-cycle corrected height error
- selected segments: A set of arrays listing the selected segments for each cycle.
- 1057 Per-cycle ATL11 output variables (see table 4-3).
- 1058 Algorithm:
- 1. Identify the segments marked as valid in *valid segs.data* and *valid segs.x slope* that are not
- members of the cycles in ref surf cycles. Label these as non ref segments.
- 2. Build **G** other, a polynomial-fitting matrix for the *non ref segments*. **G** other will include
- only the polynomial components listed in *degree\_list\_x* and *degree\_list\_y*, and (if the mission
- has been going on for at least 1.5 years) the slope-change components. Multiply **G** other by
- 1064 [ref surf/poly coeffs, ref surf/slope change rate x, ref surf/slope change rate y] to give
- 1065 corrected heights, z kc.

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- 1066 3. Take the subset of **G** other corresponding to the components in *fit cols surf* to make
- 1067 **G other surf**. Propagate the polynomial surface errors and surface-height errors for
- non ref segments based on **G\_other\_surf**, **C\_m\_surf**, and h li sigma using equation
- 1069 11. These errors are z kc sigma.
- 1070 4. Identify the segments in *non ref segments* for each cycle, and, from among these, select the
- one with the smallest z kc sigma. If, for this cycle, z kc sigma is less than 15 m, fill in the
- 1072 corresponding values of /ptx/h corr and /ptx/h corr sigma. For cycles containing no valid
- segments, report invalid data as NaN. Similarly, fill in the variables in Table 4-3, with the value
- 1074 from the segment with the smallest z kc sigma.

### 1075

### 1076 5.1.6 Calculate corrected heights for crossover data points

- **1077 Inputs:**
- 1078 *C m surf*: Covariance matrix for the reference surface model.
- 1079 *C m surf*: Covariance matrix for the reference-surface model.
- 1080 x atc ctr, y atc ctr: Center point for the surface fit, in along-track coordinates
- lat d, lon d: Latitude and longitude for the adjusted datum reference point (from /ptx/latitude,
- 1082 /ptx/longitude)
- 1083 PT: Pair track for the surface fit
- 1084 RGT: RGT for the surface fit
- 1085 ref surf/rgt azimuth: The azimuth of the RGT, relative to local north
- 1086 lat c, lon c: Location for crossover data
- 1087 time c: Time for crossover data
- 1088 h c: Elevations for crossover data
- 1089 sigma h c: Estimated errors for crossover data
- 1090 **Outputs:**
- 1091 ref pt: reference point (not for the crossing track) (ben, which one then?)
- 1092 pt: pair track for the crossing-track points
- 1093 crossing track data/rgt: Reference ground track for the crossing-track point
- 1094 crossing track data/delta time: time for the crossing-track point
- 1095 crossing track data/h corr: corrected elevation for the crossing-track points
- 1096 crossing track data/h corr sigma: error in the corrected elevation for the crossing track points
- 1097 crossing track data/h corr sigma systematic: Error component in the corrected elevation due
- 1098 to pointing and orbital errors.

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1099 crossing track data/along track rss: 1100 **Parameters:** 1101 L search XT: Across-track search distance 1102 Algorithm (executed independently for the data from each cycle of the mission): 1103 1. Project data points into the along-track coordinate system: 1104 1a: Calculate along-track and across-track vectors: 1105 x hat=[cos(ref surf/rgt azimuth), sin(ref surf/rgt azimuth)] 1106 y hat=[sin(ref surf/rgt azimuth), -cos(ref surf/rgt azimuth)] 1107 1b. Calculate the R earth, the WGS84 radius at lat d. 1108 1c: Project the crossover data points into a local projection centered on the fit 1109 center: 1110 N d= R earth (lat c-lat d) 1111 E d= R earth cos(lat d) (lon c-lon d) 1112 1d: Calculate the x and y coordinates for the data points, relative to the fit-center point: 1113  $dx c = \langle x hat, [E c, N c] \rangle$ 1114 dy c=<y hat, [E c, N c]> 1115 Here  $\langle a,b \rangle$  is the inner (dot) product of **a** and **b**. 1116 2. Calculate the fitting matrix using equation 6. 1117 3. Calculate the errors at each point using the fitting matrix and C m, using on equation 11. 1118 4. Select the minimum-error data point and report the values in Error! Reference source not 1119 found.. 1120 5. Calculate the systematic error in the corrected height: 1121 crossing track data/h sigma sigma systematic = ( sigma geo  $r^2$ + (N d ref surf/n slope)<sup>2</sup> +  $((E \ d \ ref \ surf/e \ slope)^2)^{1/2}$ 1122 6. Calculate the along-track RSS for the selected segment. For each selected crossing segment 1123 1124 calculate the endpoint heights (equal to the segment center height plus or minus 20 meters times 1125 the segment's along-track slope), and calculate the RSS of the differences between these heights 1126 and the center heights of the previous and subsequent segments. If this RSS difference is greater 1127 than 10 m for any cycle, do not report any parameters for that segment's cycle. 1128 5.1.7 Provide error-averaged values for selected ATL06 parameters 1129 **Inputs**: 1130 ATL06 data structure: ATL06 data to be averaged 1131 Selected segments: A set of arrays listing the selected segments for each cycle.

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1132 Paramteter list: A list of parameters to be averaged 1133 **Outputs:** 1134 Parameter averages: One value for each parameter and each cycle 1135 Algorithm: 1136 1. For each cycle, select the values of h li sigma based on the values within selected segments. Calculate a set of weights, w i, such that the sum of the weights is equal to 1 and each weight is 1137 1138 proportional to the inverse square of h li sigma. If only one value is present in 1139 selected segments, w I=1. 1140 2. For each parameter, multiply the weights for each cycle by the parameter values, report the 1141 averaged value in parameter averages. 1142 5.1.8 Provide miscellaneous ATL06 parameters 1143 **Inputs:** 1144 ATL06 data structure: ATL06 data to be averaged 1145 Selected segments: A set of arrays listing the selected segments for each cycle. 1146 **Outputs:** 1147 Weighted-averaged parameter values, with one value per cycle, filled in with NaN for cycles with no selected segments 1148 1149 cycle stats/h robust sprd 1150 h li rms mean (ben, I don't see this in the list) 1151 cycle stats/r eff 1152 cycle stats/tide ocean 1153 cycle stats/dac 1154 cycle stats/bsnow h 1155 cycle stats/x atc 1156 cycle stats/y atc 1157 cycle stats/sigma geo h 1158 cycle stats/sigma geo at 1159 cycle stats/sigma geo xt 1160 cycle stats/h mean 1161 Parameter minimum values, with one value per cycle, filled in NaN for cycles with no selected 1162 segments: 1163 cycle stats/cloud flg asr

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1164	cycle_stats/cloud_flg_atm
1165	cycle_stats/bsnow_conf
1166	Other parameters:
1167	cycle_stats/strong_spot: The laser beam number for the strong beam in the pair
1168	Algorithm:
1169 1170	1. Select the segments for the cycle indicated in <i>selected_segments</i> from the <i>ATL06_data_structure</i> .
1171	2: Based on <i>h_li_sigma</i> , calculate the segment weights using equation 14.
1172 1173 1174 1175	3. For ATL06 parameters h_robust_sprd, h_li_rms, r_eff, tide_ocean, dac, bsnow_h, x_atc, y_atc, sigma_geo_h, sigma_geo_at, sigma_geo_xt, and h_mean calculate the weighted average of the parameter based on the segment weights. The output parameter names are the same as the input parameter names in the cycle_stats group.
1176 1177 1178	4. For ATL06 parameters <i>cloud_flg_asr</i> and <i>cloud_flg_atm</i> report the best (minimum) value from among the selected values. For <i>bsnow_conf</i> report the maximum value from among the selected values.
1179 1180	5. For the cycle_stats/strong_spot attribute, report the laser beam number for the strong beam in the pair.
1181	
1182	5.1.9 Characterize the reference surface
1183	Inputs:
1184	poly_coeffs: Coefficients of the surface polynomial
1185	rgt_azimuth: the azimuth of the reference ground track
1186	Outputs:
1187	ref_surf/n_slope: the north component of the reference-surface slope
1188	ref_surf/e_slope: the east component of the reference-surface slope
1189	ref_surf/at_slope: the along-track component of the reference-surface slope
1190	ref_surf/xt_slope: the across-track component of the reference-surface slope
1191	ref_surf/rms_slope_fit: the rms slope of the reference surface
1192	Procedure:

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- 1. Calculate the coordinates of a grid of northing and easting offsets around the reference points,
- each between -50 m and 50 m in 10-meter increments: dN, dE
- 1195 2. Translate the coordinates into along and across-track coordinates:
- 1196  $dx=cos(rgt\ azimuth)*dN + sin(rgt\ azimuth)*dE$
- 1197  $dy=sin(rgt\_azimuth)*dN-cos(rgt\ azimuth)*dE$
- 3. Calculate the polynomial surface elevations for the grid points by evaluating the polynomial
- 1199 surface at dx and dy: z poly
- 4. Fit a plane to z poly as a function of dN and dE. The North coefficient of the plane is
- 1201 ref surf/n slope, the east component is ref surf/e slope, the RMS misfit of the plane is
- 1202 ref surf/rms slope fit. If either component of the slope has a magnitude larger than 0.2, add 2 to
- 1203 ref surf/fit quality.
- 5. Fit a plane to z poly as a function of dx and dy. The along-track coefficient of the plane is
- 1205 ref surf/at slope, the across-track component is ref surf/xt slope.

1207 6.0 APPENDIX A: GLOSSARY 1208 This appendix defines terms that are used in ATLAS ATBDs, as derived from a document 1209 circulated to the SDT, written by Tom Neumann. Some naming conventions are borrowed from 1210 Spots, Channels and Redundancy Assignments (ICESat-2-ATSYS-TN-0910) by P. Luers. 1211 Some conventions are different than those used by the ATLAS team for the purposes of making the data processing and interpretation simpler. 1212 1213 1214 **Spots.** The ATLAS instrument creates six spots on the ground, three that are weak and three that 1215 are strong, where strong is defined as approximately four times brighter than weak. These 1216 designations apply to both the laser-illuminated spots and the instrument fields of view. The 1217 spots are numbered as shown in Figure 1. At times, the weak spots are leading (when the 1218 direction of travel is in the ATLAS +x direction) and at times the strong spots are leading. 1219 However, the spot number does not change based on the orientation of ATLAS. The spots are 1220 always numbered with 1L on the far left and 3R on the far right of the pattern. Not: beams, 1221 footprints. 1222 1223 Laser pulse (pulse for short). Individual pulses of light emitted from the ATLAS laser are 1224 called laser pulses. As the pulse passes through the ATLAS transmit optics, this single pulse is split into 6 individual transmit pulses by the diffractive optical element. The 6 pulses travel to 1225 1226 the earth's surface (assuming ATLAS is pointed to the earth's surface). Some attributes of a laser 1227 pulse are the wavelength, pulse shape and duration. Not: transmit pulse, laser shot, laser fire. 1228 1229 Laser Beam. The sequential laser pulses emitted from the ATLAS instrument that illuminate 1230 spots on the earth's surface are called laser beams. ATLAS generates 6 laser beams. The laser 1231 beam numbering convention follows the ATLAS instrument convention with strong beams 1232 numbered 1, 3, and 5 and weak beams numbered 2, 4, and 6 as shown in the figures. Not: 1233 beamlet. 1234 1235 **Transmit Pulse.** Individual pulses of light emitted from the ICESat-2 observatory are called 1236 transmit pulses. The ATLAS instrument generates 6 transmit pulses of light from a single laser 1237 pulse. The transmit pulses generate 6 spots where the laser light illuminates the surface of the 1238 earth. Some attributes of a given transmit pulse are the wavelength, the shape, and the energy. 1239 Some attributes of the 6 transmit pulses may be different. Not: laser fire, shot, laser shot, laser 1240 pulse. 1241 1242 **Reflected Pulse.** Individual transmit pulses reflected off the surface of the earth and viewed by 1243 the ATLAS telescope are called reflected pulses. For a given transmit pulse, there may or may 1244 not be a reflected pulse. Not: received pulse, returned pulse.

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Photon Event. Some of the energy in a reflected pulse passes through the ATLAS receiver optics and electronics. ATLAS detects and time tags some fraction of the photons that make up the reflected pulse, as well as background photons due to sunlight or instrument noise. Any photon that is time tagged by the ATLAS instrument is called a photon event, regardless of source. Not: received photon, detected photon.

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1252 Reference Ground Track (RGT). The reference ground track (RGT) is the track on the earth at 1253 which a specified unit vector within the observatory is pointed. Under nominal operating conditions, there will be no data collected along the RGT, as the RGT is spanned by GT2L and 1254 1255 GT2R (which are not shown in the figures, but are similar to the GTs that are shown). During 1256 spacecraft slews or off pointing, it is possible that ground tracks may intersect the RGT. The 1257 precise unit vector has not yet been defined. The ICESat-2 mission has 1387 RGTs, numbered from 0001xx to 1387xx. The last two digits refer to the cycle number. Not: ground tracks, paths, 1258 1259 sub-satellite track.

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Cycle Number. Over 91 days, each of the 1387 RGTs will be targeted in the Polar Regions once. In subsequent 91-day periods, these RGTs will be targeted again. The cycle number tracks the number of 91-day periods that have elapsed since the ICESat-2 observatory entered the science orbit. The first 91-day cycle is numbered 01; the second 91-day cycle is 02, and so on. At the end of the first 3 years of operations, we expect the cycle number to be 12. The cycle number will be carried in the mid-latitudes, though the same RGTs will (in general) not be targeted more than once.

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**Sub-satellite Track (SST).** The sub-satellite track (SST) is the time-ordered series of latitude and longitude points at the geodetic nadir of the ICESat-2 observatory. In order to protect the ATLAS detectors from damage due to specular returns, and the natural variation of the position of the observatory with respect to the RGT throughout the orbit, the SST is generally not the same as the RGT. Not: reference ground track, ground track.

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Ground Tracks (GT). As ICESat-2 orbits the earths, sequential transmit pulses illuminate six ground tracks on the surface of the earth. The track width is approximately 10m wide. Each ground track is numbered, according to the laser spot number that generates a given ground track. Ground tracks are therefore always numbered with 1L on the far left of the spot pattern and 3R on the far right of the spot pattern. Not: tracks, paths, reference ground tracks, footpaths.

1280

Reference Pair Track (RPT). The reference pair track is the imaginary line halfway between the planned locations of the strong and weak ground tracks that make up a pair. There are three RPTs: RPT1 is spanned by GT1L and GT1R, RPT2 is spanned by GT2L and GT2R (and may be coincident with the RGT at times), and RPT3 is spanned by GT3L and GT3R. Note that this is

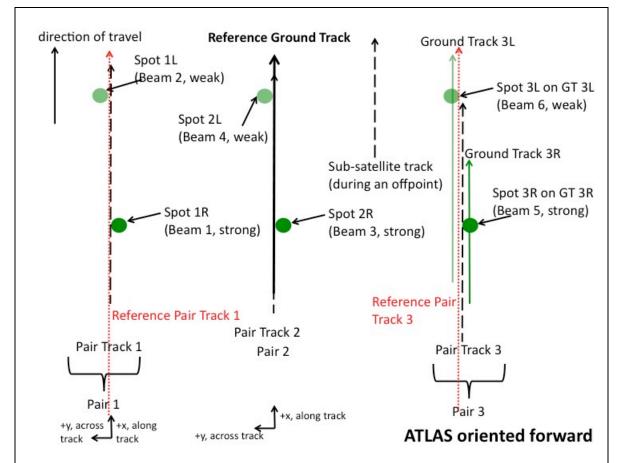
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1285 1286	the planned location of the midway point between GTs. We will not know this location very precisely prior to launch. Not: tracks, paths, reference ground tracks, footpaths, pair tracks.
1287	
1288 1289 1290 1291 1292 1293	<b>Pair Track (PT).</b> The pair track is the imaginary line half way between the actual locations of the strong and weak ground tracks that make up a pair. There are three PTs: PT1 is spanned by GT1L and GT1R, PT2 is spanned by GT2L and GT2R (and may be coincident with the RGT at times), and PT3 is spanned by GT3L and GT3R. Note that this is the actual location of the midway point between GTs, and will be defined by the actual location of the GTs. Not: tracks, paths, reference ground tracks, footpaths, reference pair tracks.
1294	
1295 1296 1297 1298	<b>Pairs.</b> When considered together, individual strong and weak ground tracks form a pair. For example, GT2L and GT2R form the central pair of the array. The pairs are numbered 1 through 3: Pair 1 is comprised of GT1L and GT1R, pair 2 is comprised of GT2L and GT2R, and pair 3 is comprised of GT3L and 3R.
1299	
1300 1301 1302 1303	<b>Along-track.</b> The direction of travel of the ICESat-2 observatory in the orbit frame is defined as the along-track coordinate, and is denoted as the +x direction. The positive x direction is therefore along the Earth-Centered Earth-Fixed velocity vector of the observatory. Each pair has a unique coordinate system, with the +x direction aligned with the Reference Pair Tracks.
1304	
1305 1306	<b>Across-track.</b> The across-track coordinate is y and is positive to the left, with the origins at the Reference Pair Tracks.
1307	
1308 1309 1310 1311 1312	<b>Segment.</b> An along-track span (or aggregation) of PE data from a single ground track or other defined track is called a segment. A segment can be measured as a time duration (e.g. from the time of the first PE to the time of the last PE), as a distance (e.g. the distance between the location of the first and last PEs), or as an accumulation of a desired number of photons. Segments can be as short or as long as desired.
1313	
1314	Signal Photon. Any photon event that an algorithm determines to be part of the reflected pulse.
1315	
1316 1317 1318 1319	<b>Background Photon.</b> Any photon event that is not classified as a signal photon is classified as a background photon. Background photons could be due to noise in the ATLAS instrument (e.g. stray light, or detector dark counts), sunlight, or mis-classified signal photons. Not: noise photon.
1320	

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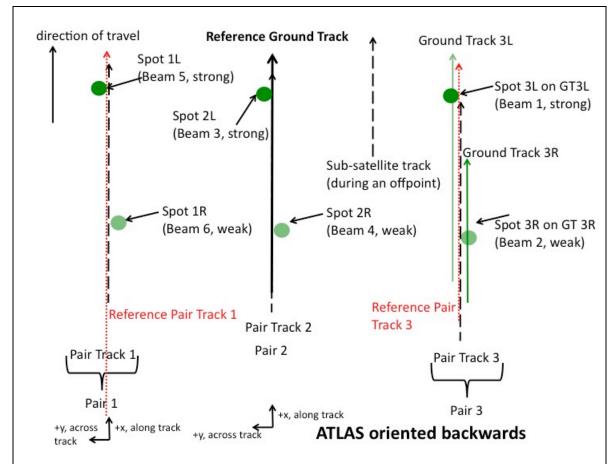
1321 1322 1323 1324 1325 1326	<b>h_**.</b> Signal photons will be used by higher-level products to determine height above the WGS-84 reference ellipsoid, using a semi-major axis (equatorial radius) of 6378137m and a flattening of 1/298.257223563. This can be abbreviated as 'ellipsoidal height' or 'height above ellipsoid'. These heights are denoted by h; the subscript ** will refer to the specific algorithm used to determine that elevation (e.g. is = ice sheet algorithm, si = sea ice algorithm, etc). Not: elevation.
1327	
1328 1329	<b>Photon Cloud.</b> The collection of all telemetered photon time tags in a given segment is the (or a) photon cloud. Not: point cloud.
1330	
1331 1332 1333 1334	<b>Background Count Rate.</b> The number of background photons in a given time span is the background count rate. Therefore a value of the background count rate requires a segment of PEs and an algorithm to distinguish signal and background photons. Not: Noise rate, background rate.
1335	
1336 1337 1338 1339	<b>Noise Count Rate.</b> The rate at which the ATLAS instrument receives photons in the absence of any light entering the ATLAS telescope or receiver optics. The noise count rate includes PEs due to detector dark counts or stray light from within the instrument. Not: noise rate, background rate, and background count rate.
1340	
1341 1342 1343 1344 1345 1346 1347 1348	<b>Telemetry band.</b> The subset of PEs selected by the science algorithm on board ATLAS to be telemetered to the ground is called the telemetry band. The width of the telemetry band is a function of the signal to noise ratio of the data (calculated by the science algorithm onboard ATLAS), the location on the earth (e.g. ocean, land, sea ice, etc), and the roughness of the terrain, among other parameters. The widths of telemetry bands are adjustable on-orbit. The telemetry bandwidth is described in Section 7 or the ATLAS Flight Science Receiver Algorithms document. The total volume of telemetered photon events must meet the data volume constraint (currently 577 GBits/day).
1349	
1350 1351 1352 1353	<b>Window, Window Width, Window Duration.</b> A subset of the telemetry band of PEs is called a window. If the vertical extent of a window is defined in terms of distance, the window is said to have a width. If the vertical extent of a window is defined in terms of time, the window is said to have a duration. The window width is always less than or equal to the telemetry band.
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Figure 6-1. Spots and tracks, forward flight



Spot and track naming convention with ATLAS oriented in the forward (instrument coordinate +x) direction.

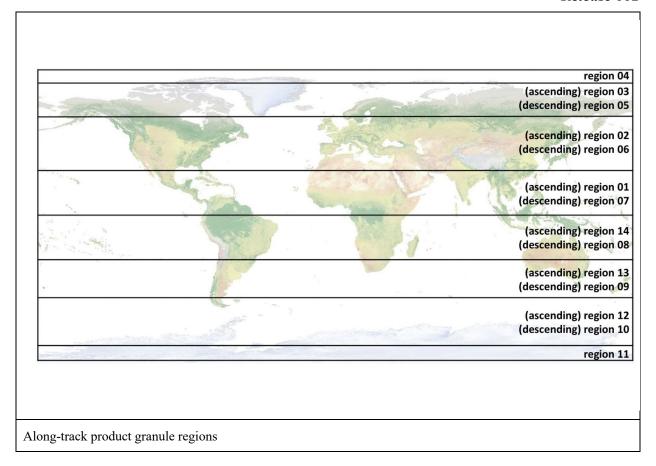
Figure 6-2. Spots and tracks, backward flight



Spot and track naming convention with ATLAS oriented in the backward (instrument coordinate -x) direction.

Figure 6-3. Granule regions

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#### 7.0 BROWSE PRODUCTS

For each ATL11 data file, there will be eight figures written to an associated browse file. Two of these figures are required and are located in the default group; default1 and default2. The browse filename has the same pattern as the data filename, namely,

ATL11\_ttttss\_c1c2\_rr\_vVVV\_BRW.h5, where tttt is the reference ground track, ss is the orbital segment, c1 is the first cycle of data in the file, c2 is the last cycle of data in the file, rr is the release and VVV is the version. Optionally, the figures can also be written to a pdf file.

Below is a discussion of the how the figures are made, with examples from the data file ATL11\_009403\_0307\_02\_vU07.h5. Note that the figure numbering in this section is distinct from that in the rest of the document; the figures shown here are labeled as they are in each browse-product file.

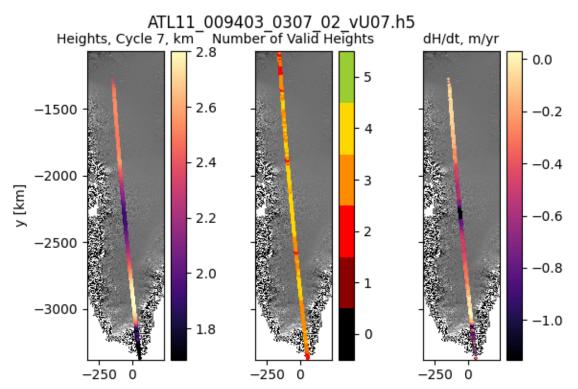


Figure 1. Height data, in km, from cycle 7 (1st panel). Number of cycles with valid height data (2nd panel). Change in height over time, in meters/year, cycle 7 from cycle 3 (3rd panel). All overlaid on gradient of DEM. x, y in km. Maps are plotted in a polar-stereographic projection with a central longitude of 45W and a standard latitude of 70N.

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1387 The background for the three panels in Figure 1 is the gradient DEM in gray scale. It is shown in 1388 a polar-stereographic projection with a central longitude of 45W (0E) and a standard latitude of 1389 70N (71S), for the Northern (Southern) Hemisphere. The map is bounded by the extent of height 1390 data plus a buffer. ATL11 heights (/ptx/h corr) from all pairs of the latest cycle with valid data, here cycle 7, are plotted in the first panel. The "magma" color map indicates the heights in km. 1391 1392 The limits on the color bar are set with the python scipy.stat.scoreatpercentile method at 5% and 1393 95%. In the second panel are plotted the number of valid heights summed over all cycles at each 1394 location. The color bar extends to the total number of cycles in the data file. The change in height over time, dH/dt, is plotted in the third panel, in meters/year. dHdt is the change in height of the 1395 last cycle with valid data from the first cycle with valid data (/ptx/h corr) divided by the 1396 1397 associated times (/ptx/delta time). Text of 'No Data' is printed in the panel if there is only one 1398 cycle with valid data, or if the first and last cycles with valid data have no common reference 1399 point numbers (/ptx/ref pt). All plots are in x,y coordinates, in km. This figure is called

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# ATL11\_009403\_0307\_02\_vU07.h5

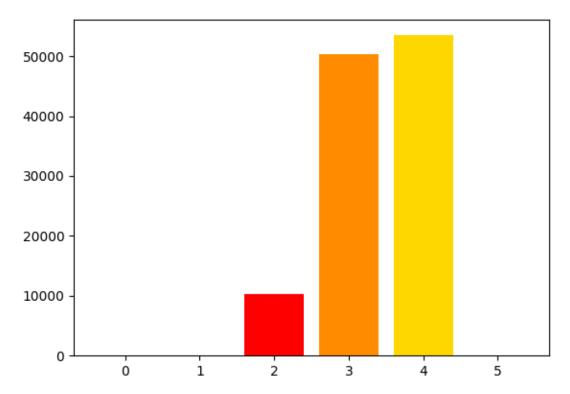


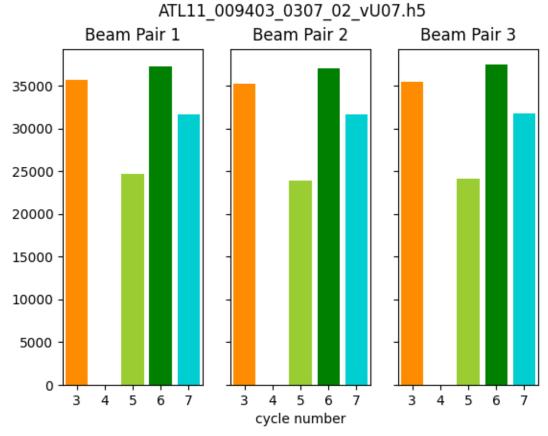
Figure 2. Histogram of number of cycles with valid height measurements, all beam pairs.

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default/default1 in the BRW.h5 file.

A histogram of the number of valid height measurements (/ptx/h\_corr) is in Figure 2. Valid height data are summed across all cycles, for each reference point number (/ptx/ref\_pt). The color scale is from zero to the total number of cycles in the data file and matches those in Figure 1, 2<sup>nd</sup> panel. This figure is called validrepeats\_hist in the BRW.h5 file.

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Figure 3. Number of valid height measurements from each beam pair.

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Histograms in Figure 3 show the number of valid heights (/ptx/h\_corr) for each cycle, separated by beam pair. The cycle numbers are color coded. This figure is called default/default2 in the BRW.h5 file.

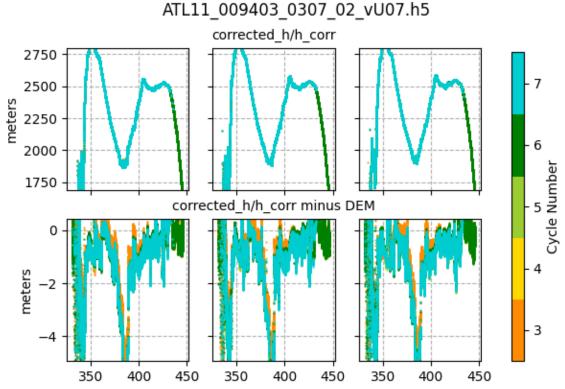


Figure 4. Top row: Heights, in meters, plotted for each beam pair: 1 (left), 2 (center), 3 (right). Bottom row: Heights minus DEM, in meters. Y-axis limits are scores at 5% and 95%. Color coded by cycle number. Plotted against reference point number/1000.

There are six panels in Figure 4, with two rows and three columns. In the top row are plotted the height measurements (/ptx/h\_corr) for each beam pair, one pair per panel. In the bottom row are plotted the same height measurements minus the collocated DEM (ref\_surf/dem\_h) values, one pair per panel. The plots are color coded by cycle number, as in Figure 3. The heights are plotted versus reference point number (/ptx/ref\_pt) divided by 1000 for a cleaner plot. The y-axis is in meters for both rows. The y-axis limits for the top and bottom rows are set separately, using the python scipy.stats.scoreatpercentile method with limits of 5% and 95% for heights and height differences, respectively. Text of 'No Data' is printed in a panel if there are no valid height data for that pair. This figure is called h corr h corr-DEM in the BRW.h5 file.

# ATL11 009403 0307 02 vU07.h5 height-DEM: Cycle 3 Cycle 4 5000 2500 0 Cycle 5 Cycle 6 5000 2500 0 Cycle 7 5000 2500 0 -2 -4 -2 -4 0

Figure 5. Histograms of heights minus DEM heights, in meters. One histogram per cycle, all beam pairs. X-axis limits are the scores at 5% and 95%.

Figure 5 is associated with Figure 4. It is a multi-paneled figure, with the number of panels dependent on the number of cycles in the data file. Each panel is a histogram of the heights (/ptx/h\_corr) minus collocated DEM heights (ref\_surf/dem\_h) color coded by cycle, the same as in Figures 3 and 4. The limits on the histograms are set using the python scipy.stats.scoreatpercentile method with limits of 5 and 95% for all cycles of data, the same values used in Figure 4 bottom row. This figure is called h corr-DEM hist in the BRW.h5 file.

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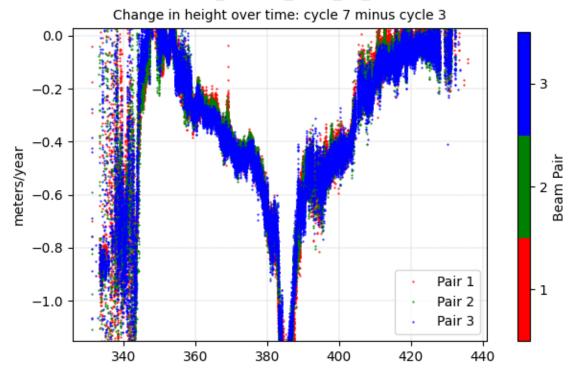


Figure 6. Change in height over time, dH/dt, in meters/year. dH/dt is cycle 7 from cycle 3. Color coded by beam pair: 1 (red), 2 (green), 3 (blue). Y-axis limits are scores at 5% and 95%. Plotted against reference point number/1000.

The changes in height with time, dH/dt, in meters/year are plotted in Figure 6. The calculation differences the first and last cycles with valid height data (/ptx/h\_corr) divided by the associated time differences (/ptx/delta\_time). The change in heights for pair 1 are in red, for pair 2 are in green and for pair 3 are in blue. The y-axis limits are set using the python scipy.stats.scoreatpercentile method with limits of 5% and 95%. The x-axis is reference point number (/ptx/ref\_pt) divided by 1000 for a cleaner plot. Text of 'No Data' is printed in the panel if there is only one cycle with valid data, or if the first and last cycles with valid data have no common reference point numbers. This figure is called dHdt in the BRW.h5 file.

## Release 002

## 1448 Glossary/Acronyms

ASAS	ATLAS Science Algorithm Software
ATBD	Algorithm Theoretical Basis Document
ATLAS	ATLAS Advance Topographic Laser Altimeter System
CDF	Cumulative Distribution Function
DEM	Digital Elevation Model
GSFC	Goddard Space Flight Center
GTs	Ground Tracks
ICESat-2	Ice, Cloud, and Land Elevation Satellite-2
IKR	I Know, Right?
MABEL	Multiple altimeter Beam Experimental Lidar
MIS	Management Information System
NASA	National Aeronautics and Space Administration
PE	Photon Event
POD	Precision Orbit Determination
PPD	Precision Pointing Determination
PRD	Precise Range Determination
PSO	ICESat-2 Project Science Office
PTs	Pair Tracks
RDE	Robust Dispersion Estimate
RGT	Reference Ground Track
RMS	Root Mean Square
RPTs	Reference Pair Tracks

Release 002

RT Real Time

SCoRe Signature Controlled Request

SIPS ICESat-2 Science Investigator-led Processing System

TLDR Too Long, Didn't Read

TBD To Be Determined

# Release 002

1449	References
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